

# Electronic passport and biometrics, winter 2006

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## 5. Exercise sheet

Hand in solutions until Tuesday, 5 December, 12<sup>15</sup>.

**Exercise 5.1** (A simple linear attack).

(4+4 points)

Each variable in the following stores one byte or eight bits. Consider the function

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$$f(B, C) = B \oplus C,$$

$K_j = 0x42$  for all relevant  $j$ , and let  $(H_1, H_2, H_3)$  be computed as follows

**Algorithm.**

Input: A message  $(X_0, X_1, X_2, \dots, X_{n-1})$ .

Output: A hash value  $H \in \{0, 1\}^{3 \times 8}$ .

1.  $(H_1, H_2, H_3) \leftarrow (0, 0, 0)$ .
2. **For**  $i = 0..n - 1$  **do** 3–7
3.      $(A, B, C) \leftarrow (H_1, H_2, H_3)$ .
4.     **For**  $j = 0..R - 1$  **do** 5–6
5.          $t \leftarrow A \otimes 2 + f(B, C) + X_{i+j} + K_j$ ,
6.          $(A, B, C) \leftarrow (t, A, B \otimes 1)$ .
7.      $(H_1, H_2, H_3) \leftarrow (H_1 + A, H_2 + B, H_3 + C)$ .
8. **Return**  $H_1|H_2|H_3$ .

We consider a message with  $n = 1$  and for simplicity we use  $R = 1$ . Write one of the bits in the output as a function in the input bits in  $X_0$  in the form  $f(X_{00}, \dots, X_{07}) = a_0X_{00} + \dots + a_7X_{07} + a_8$  where  $a_i \in \{0, 1\}$  as good as possible. Can you find coefficients  $a_i$  such that  $f$  and the chosen output bit coincide in, say 75% of all cases?

Try  $R = 2$ .

+4

**Exercise 5.2 (Biometrics).**

(3+2 points)

Consider a chip card that stores your finger prints.

- 1 (i) Say, the false accept rate is 3%. Where does this induce problems?
- 1 (ii) Say, the false reject rate is 5%. Where does this induce problems?
- 1 (iii) Who can benefit from getting this information?
- +1 (iv) What kind of protection should be employed?
- +1 (v) Do you think people will accept such a card?