

Electronic passport and biometrics, winter 2006

MICHAEL NÜSKEN

5. Exercise sheet

Hand in solutions until Tuesday, 5 December, 12¹⁵.

Exercise 5.1 (A simple linear attack).

(4+4 points)

Each variable in the following stores one byte or eight bits. Consider the function

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$$f(B, C) = B \oplus C,$$

$K_j = 0x42$ for all relevant j , and let (H_1, H_2, H_3) be computed as follows

Algorithm.

Input: A message $(X_0, X_1, X_2, \dots, X_{n-1})$.

Output: A hash value $H \in \{0, 1\}^{3 \times 8}$.

1. $(H_1, H_2, H_3) \leftarrow (0, 0, 0)$.
2. **For** $i = 0..n - 1$ **do** 3–7
3. $(A, B, C) \leftarrow (H_1, H_2, H_3)$.
4. **For** $j = 0..R - 1$ **do** 5–6
5. $t \leftarrow A \otimes 2 + f(B, C) + X_{i+j} + K_j$,
6. $(A, B, C) \leftarrow (t, A, B \otimes 1)$.
7. $(H_1, H_2, H_3) \leftarrow (H_1 + A, H_2 + B, H_3 + C)$.
8. **Return** $H_1|H_2|H_3$.

We consider a message with $n = 1$ and for simplicity we use $R = 1$. Write one of the bits in the output as a function in the input bits in X_0 in the form $f(X_{00}, \dots, X_{07}) = a_0X_{00} + \dots + a_7X_{07} + a_8$ where $a_i \in \{0, 1\}$ as good as possible. Can you find coefficients a_i such that f and the chosen output bit coincide in, say 75% of all cases?

Try $R = 2$.

+4

Exercise 5.2 (Biometrics).

(3+2 points)

Consider a chip card that stores your finger prints.

- 1 (i) Say, the false accept rate is 3%. Where does this induce problems?
- 1 (ii) Say, the false reject rate is 5%. Where does this induce problems?
- 1 (iii) Who can benefit from getting this information?
- +1 (iv) What kind of protection should be employed?
- +1 (v) Do you think people will accept such a card?