

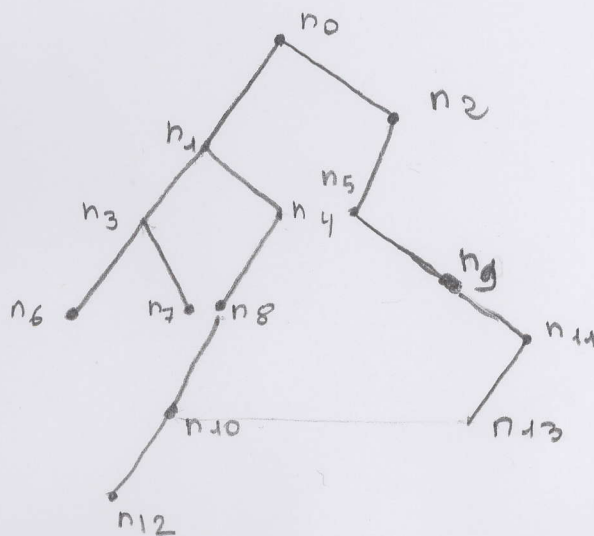
### 1 - Mathematical properties of binary trees:

prove that the internal path length of a binary tree with  $N$  internal nodes is at least  $N \log \frac{N}{4}$  and at most  $\frac{N(N-1)}{2}$ .

hint: Use the fact that the external path of a binary tree with  $N$  internal nodes is  $\geq N$  greater than its internal path length.

### 2 - Tree Traversal:

Perform the preorder, inorder and post order traversals of the following tree:



### 3 - Implementation

Implement the post order traversal of a binary tree.