

Lecture Notes
electronic passports & biometrics

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trust

ICAO

Passport

authentication

identification

special paper
with specific
fine pattern

unique id-number

hologram

issuing authority
(state)

total number of pages

biometry

seal
signature

· remarks
· accompanying
persons...

date of validity
& (expiration)
of issuance

immigration notes
emigration notes
visas

trusted parties

fingerprint

electronic
cryptographic

chip → RFID
→ contact
chip

MRZ machine
readable
zone

- magnetic stripe

- barcode

electronic
signature

encryption

person

nationality
country

name

date of birth

place of birth

- current address

- father's name
- mother's name

photograph

eyes:
· retina scan
· iris scan

eye color
- hair color

- weight
height

gender

voice

signature

Table IIIA-1. Summary of security recommendations

Threats	Basic features	Additional features
Counterfeiting		
Paper substrates (5.1.1)	<ul style="list-style-type: none"> – controlled UV response – two-tone watermark – chemical sensitizers – appropriate absorbency and surface characteristics 	<ul style="list-style-type: none"> – registered watermark – invisible UV fibres/planquettes – visible UV fibres/planquettes – embedded or window thread
Label substrates (5.1.2)	<ul style="list-style-type: none"> – controlled UV response – chemical sensitizers – invisible UV fibres/planquettes – visible UV fibres/planquettes – non-peelable adhesive 	<ul style="list-style-type: none"> – embedded or window thread
Plastic/synthetic substrates (5.1.4)	<ul style="list-style-type: none"> – as per paper or substitute – security features providing an equivalent level of security in plastic 	<ul style="list-style-type: none"> – optically variable feature(OVF)
Security printing (5.2)	<ul style="list-style-type: none"> – two-colour guilloche background – rainbow printing – anti-scan pattern – microprinting – unique biodata page design 	<ul style="list-style-type: none"> – intaglio printing – latent image – duplex pattern – 3-D design feature – front-to-back register feature – deliberate error in microprint – unique design on every page – tactile feature
Numbering (5.2.3)	<ul style="list-style-type: none"> – unique document number 	<ul style="list-style-type: none"> – perforated document number – special typefonts
Inks (5.2.2):	<ul style="list-style-type: none"> – UV inks on all pages – reactive inks 	<ul style="list-style-type: none"> – optically variable properties – metallic inks – penetrating numbering ink – metamerik inks – infrared dropout ink – thermochromic ink – photochromic ink – infrared fluorescent ink – phosphorescent ink – tagged ink

Table IIIA-1. Summary of security recommendations

Threats	Basic features	Additional features
Photo-substitution (5.4.4)	<ul style="list-style-type: none"> – integrated biodata page – guilloche overlapping portrait – secure laminate or equivalent 	<ul style="list-style-type: none"> – OVF over the portrait – digital signature in document – embedded image – secondary portrait image – storage and retrieval system for digital portrait images – biometric feature
Alteration of the biodata (5.4.4)	<ul style="list-style-type: none"> – reactive inks – secure laminate or equivalent 	<ul style="list-style-type: none"> – chemical sensitizers in substrate – secondary biodata image – OVF over the biodata
Page substitution (5.5.3/4)	<ul style="list-style-type: none"> – lock stitch or equivalent – unique biodata page design 	<ul style="list-style-type: none"> – programmable sewing pattern – fluorescent sewing thread – serial number on every page – page folio numbers in guilloche – index marks on every page – biodata on inside page
Deletion/removal of stamps and labels (5.5.5)	<ul style="list-style-type: none"> – reactive inks – chemical sensitizers – high-tack adhesives (labels) – permanent inks (stamps) 	<ul style="list-style-type: none"> – over-lamination – high absorbency substrates – frangible substrate (labels)
Document theft (5.7.1):	<ul style="list-style-type: none"> – good physical security arrangements – control of all security components – serial numbers on blank documents – secure transport of blank documents – internal fraud protection system – international exchange on lost and stolen documents 	<ul style="list-style-type: none"> – CCTV in production areas – centralized production – digital signature – embedded image

Cryptographic passports

Security?

- difficult to forge
- impossible to forge — Unrealistic
- difficult to ~~access~~ read for unauthorized parties
- difficult to track
- database?
- discrimination?

Reliability?

- easy to use

- Acceptance?
- Accessibility? Costs?
- Robust?

> biometric
false accept rates
false reject rates

Inlay with integrated
contactless chip

Passport cover

laminated
protective layer

Data page with
data and photograph

Inlay with
contactless chip

laminated
protective layer

Contactless module

Integrated Circuit

Antenna

► The contactless chip can be integrated into either the cover page or the data page.

New threat due to
contactless chip:

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(2)

invisible reading process,
radio waves are not visible!

→ USE CRYPTOGRAPHY!

Starting ideas:

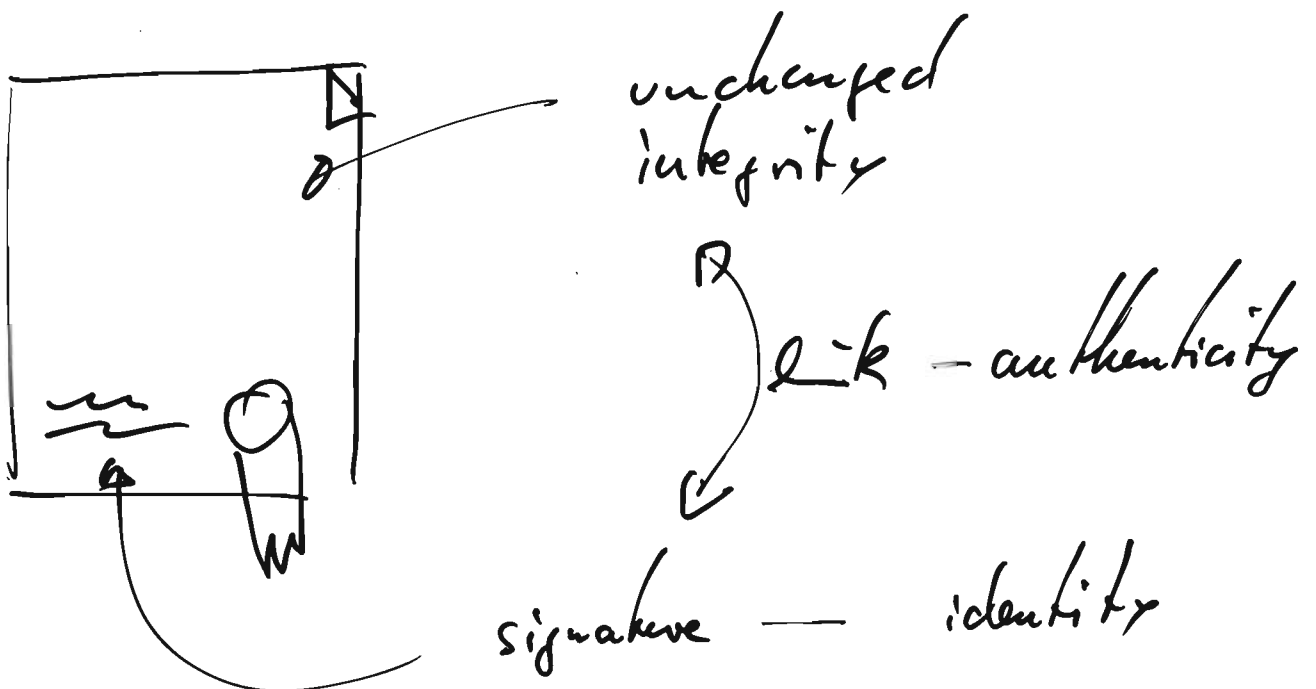
- use MRZ for basic access control
... How? Details ...
- use additional barriers for access
to sensitive data, like e.g. finger prints.

Signatures til ECDSA

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22.4.09
①

What's a signature?

- identification of a person
(unique, every person has a different one)
use biometrics...
- authenticates a document
(commitment, sign a document)
 - Link between person and document
which cannot be separated.
- integrity of the document



ElGamal type signatures, first try

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$$a^b b^8 = g^m$$

verification equation

What is necessary to give this some sense?

→ need a multiplication for the parts/elements

$$a^b, b^8$$

→ need an exponentiation to compute

$$a^b, b^8, g^m$$

Constraint: everything must be finite!

Use a finite group!

Excursion: finite groups.

Computer scientist's definition:

⒫roper: there is an implementation which allows a finite set G of values and has an operation $\cdot: G \times G \rightarrow G$ and (optionally) an operation $\text{inv} = ?^{-1}: G \rightarrow G$

and (optionally) an element 1 cpb
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$$1 \in G$$

(A)ssociative: for any $a, b, c \in G$:

$$(a \cdot b) \cdot c = a \cdot (b \cdot c)$$

(N)eutral element: for any $a \in G$ we have

$$1 \cdot a = a = a \cdot 1$$

(I)nverses : for any $a \in G$ there exists $b \in G$

$$a \cdot b = 1 = b \cdot a$$

or equiv: for any $a \in G$ we have

$$a \cdot a^{-1} = 1 = a^{-1} \cdot a$$

optional:

(C)ommutative : for any $a, b \in G$ we have

$$a \cdot b = b \cdot a$$

Examples:

$(\mathbb{Z}_N, +)$: elements are coded as integer $0, 1, 2, \dots, N-1$ and the operation is defined by:

$$a + b := (\overset{\vee}{a} + \overset{\vee}{b}) \bmod N \in \mathbb{Z}_N$$

$$\text{[in contrast to: } (\overset{\vee}{a} + \overset{\vee}{b}) \bmod N \in \mathbb{Z} \text{ .]}$$

in \mathbb{Z}_{15} : $9 + 7 = 1$

(\mathbb{Z}_N, \cdot) , $N=6$. Not a group:
no inverse for 2:

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④

$$\begin{array}{ll} 2 \cdot 0 = 0, & 2 \cdot 3 = 0, \\ 2 \cdot 1 = 2, & 2 \cdot 4 = 2 \\ 2 \cdot 2 = 4, & 2 \cdot 5 = 4. \end{array}$$

(\mathbb{Z}_N, \cdot) , $N=7$. Not a group!

Beck: $\begin{array}{l} 2 \cdot 4 = 1, \\ 3 \cdot 5 = 1, \\ 1 \cdot 1 = 1, \\ 6 \cdot 6 = 1. \end{array}$

$0 \cdot a = 0$ never $1 \rightarrow$ no inverse.

$(\mathbb{Z}_N \setminus \{0\}, \cdot)$, $N=7$.

\cdot	1	2	3	4	5	6
1	1	2	3	4	5	6
2	2	4	6	1	3	5
3	3	6	2	5	1	4
4	4	1	5	2	6	3
5	5	3	1	6	4	2
6	6	5	4	3	2	1

Proper: \checkmark (Check the table!)

Associative: We know that multiplication for integers is associative:

$$\begin{aligned} (a \cdot b) \cdot c &= (\underbrace{\tilde{a} \cdot \tilde{b}}_{\tilde{z}} \underbrace{\text{rem } N}) \cdot \tilde{c} \pmod{N} \\ &= (\underbrace{\tilde{a} \cdot \tilde{b} - k \cdot N}_{\tilde{z}}) \cdot \tilde{c} \pmod{N} \end{aligned}$$

$(\mathbb{Z}_6 \setminus \{0\}, \cdot)$ not a group!

Qb
22.4.05
⑥

Still: 2 has no inverse.

Also: $2 \cdot 3 \notin \mathbb{Z}_6 \setminus \{0\}$.

$(\mathbb{Z}_N^\times, \cdot)$

↑ set of invertible elements in \mathbb{Z}_N .

P? A ✓ N: 1 is invertible I: ? ✓
 $\rightarrow 1 \cdot 1 = 1$ (invertible)
 $1 \cdot a = a$ (neutral)

I: We have to check that if a is invertible, then its inverse b is also invertible.

But if: $a \cdot b = 1 = b \cdot a$
 $b \cdot a = 1 = a \cdot b$

Then:
so a is the inverse of b
and thus b is invertible.

P: Given a, b invertible.
check that $a \cdot b$ is invertible.

But: $(a \cdot b) \cdot (b^{-1} \cdot a^{-1}) = 1$
 $(b^{-1} \cdot a^{-1}) \cdot (a \cdot b) = 1 \checkmark$

This is a group! We call it:
the unit group of integers modulo N .

$$\begin{aligned}
 (a \cdot b) \cdot c &= \left(\begin{pmatrix} \check{a} & \check{b} \\ \check{z} & \check{z} \end{pmatrix} \cdot \check{c} \right) \bmod N - \underbrace{\left(\begin{pmatrix} \check{b} & \check{c} \\ \check{z} & \check{z} \end{pmatrix} \right) \bmod N}_{\substack{\text{is a multiple} \\ \text{of } N}} \bmod N \quad \left. \begin{array}{l} \text{cpb} \\ 22.409 \\ \textcircled{5} \end{array} \right\} \\
 &= \begin{pmatrix} \check{a} & \check{b} \\ \check{z} & \check{z} \end{pmatrix} \cdot \check{c} \bmod N \\
 &= \check{a} \cdot \begin{pmatrix} \check{b} & \check{c} \\ \check{z} & \check{z} \end{pmatrix} \bmod N \\
 &= a \cdot (b \cdot c)
 \end{aligned}$$

Neutral: $1 \in \mathbb{Z}_N \setminus \{0\}$.

$$\begin{aligned}
 1 \cdot a &= \begin{pmatrix} \check{1} & \check{a} \\ \check{z} & \check{z} \end{pmatrix} \bmod N \\
 &= \check{a} \bmod N = a.
 \end{aligned}$$

Inverses: Every row has a 1. ✓

Commutative? Table symmetric w.r.t to the diagonal.

$$\begin{aligned}
 \text{Here: } a \cdot b &= \begin{pmatrix} \check{a} & \check{b} \\ \check{z} & \check{z} \end{pmatrix} \bmod N \\
 &= \begin{pmatrix} \check{b} & \check{a} \\ \check{z} & \check{z} \end{pmatrix} \bmod N \\
 &= b \cdot a.
 \end{aligned}$$

Summary: $(\mathbb{Z}_7 \setminus \{0\}, \cdot)$ is a comm. group. !

Example

$$\mathbb{Z}_6^{\times} = (\{1, 5\}, \cdot) \\ \cong (\mathbb{Z}_2, +)$$

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⑦

$$\begin{array}{c|cc} & 1 & 5 \\ \hline 1 & 1 & 5 \\ 5 & 5 & 1 \end{array}$$

$$\begin{array}{c|cc} + & 0 & 1 \\ \hline 0 & 0 & 1 \\ 1 & 1 & 0 \end{array}$$

$$(\mathbb{Z}_2, +) \longrightarrow (\mathbb{Z}_6^{\times}, \cdot)$$

$$\begin{array}{lcl} 0 & \longmapsto & 1 \\ 1 & \longmapsto & 5 \end{array}$$

$$a \longmapsto 5^a$$

$$\check{0} = 0 \in \mathbb{Z}$$

$$\check{1} = 1 \in \mathbb{Z}$$

fast?!

← ?? we do not know,
a fast algorithm!

Example

$$\mathbb{Z}_5^{\times} = (\{1, 2, 3, 4\}, \cdot) \cong (\mathbb{Z}_4, +)$$

$$\mathbb{Z}_4^{\times} = (\{1, 3\}, \cdot) \cong (\mathbb{Z}_2, +)$$

$$\mathbb{Z}_7^{\times} = (\{1, 2, 3, 4, 5, 6\}, \cdot) \cong (\mathbb{Z}_6, +)$$

$$\mathbb{Z}_8^{\times} = (\{1, 3, 5, 7\}, \cdot) \cong (\mathbb{Z}_2 \times \mathbb{Z}_2, +)$$

$$\mathbb{Z}_9^{\times} = (\{1, 2, 4, 5, 7, 8\}, \cdot) \cong (\mathbb{Z}_6, +)$$

$$\stackrel{1/2}{\cong} (\mathbb{Z}_2 \times \mathbb{Z}_3, +)$$

How to compute and/or decide inverses?

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(2)

Task: Given $a \in \mathbb{Z}_N$.

Find $b \in \mathbb{Z}_N$ such that

(*) $a \cdot b = 1$ (in \mathbb{Z}_N),
or prove there is no such b .

Notice that (*) is equivalent to

$$\exists b \in \mathbb{Z} : \overset{v}{a} \cdot \overset{v}{b} + \overset{k}{N} \cdot N = 1$$

So we look for

$$\overset{v}{b}, k \in \mathbb{Z} : \overset{v}{b} \cdot \overset{v}{a} + \overset{k}{N} \cdot N = 1 \text{ in } \mathbb{Z}$$

Rephrased: find b, k such that

$$b \cdot \overset{v}{a} + k \cdot N$$

is (positive and) as small as possible!

For example:

$$\begin{aligned} 1 \cdot \overset{v}{a} + 0 \cdot N &= \overset{v}{a} \\ 0 \cdot \overset{v}{a} + 1 \cdot N &= N \end{aligned}$$

Example: $N=9, \overset{v}{a}=2$. Starting:

$$\begin{array}{lll} \textcircled{1} & \textcircled{1} \cdot 2 + \textcircled{0} \cdot 9 & = \textcircled{2} \\ \textcircled{2} & \textcircled{0} \cdot 2 + \textcircled{1} \cdot 9 & = \textcircled{9} \\ \textcircled{2} - \textcircled{1} & (-1) \cdot 2 + 1 \cdot 9 & = 7 \\ \textcircled{2} - 4 \cdot \textcircled{1} & (-4) \cdot 2 + 1 \cdot 9 & = 1 \end{array}$$

Extended Euclidean Algo on Them

pb
22.4.09

(9)

$15 \in \mathbb{Z}_{87}$ Inverse?

r	q	s	t	
<u>87</u>	.	<u>1</u>	<u>0</u>	$3 \cdot 87 + 1 \cdot 15 = r$
$\rightarrow 15$	5	0	1	$1 \cdot 87 + 0 \cdot 15 = 87$
$(87) - 5 \cdot (15): 12$	1	1	-5	$0 \cdot 87 + 1 \cdot 15 = 15$
$(15) - 1 \cdot (12): 3$	4	-1	6	$1 \cdot 87 + (-5) \cdot 15 = 12$
0		5	-29	$(-1) \cdot 87 + 6 \cdot 15 = 3$
				$5 \cdot 87 + (-29) \cdot 15 = 0$

$14 \in \mathbb{Z}_{32}$ Inverse?

Eurocrypt 2009

Conference Program 26. - 30. April 2009

April 26, 2009 Sunday

10:00 – 17:00 Board Meeting (only IACR Board members)

17:00 – 21:00 Welcome Reception and Registration

April 27, 2009 Monday

08:30 Registration Desk open

09:00 – 09:15 Welcome / Opening Remarks

Session 1
09:15 – 10:55 Security, Proofs and Models I

09:15 – 09:40 Possibility and Impossibility Results for Encryption and Commitment Secure under Selective Opening.
Mihir Bellare, Dennis Hofheinz, Scott Yilek

09:40 – 10:05 Breaking RSA Generically is Equivalent to Factoring
Divesh Aggarwal, Ueli Maurer

10:05 – 10:30 Resettably Secure Computation
Vipul Goyal, Amit Sahai

10:30 – 10:55 On the Security Loss in Cryptographic Reductions
Chi-Jen Lu

10:55 – 11:25 Coffee Break

Invited Talk
11:25 – 12:25 Practice-Oriented Provable-Security and the Social Construction of Cryptography
Phillip Rogaway

12:45 – 13:45 Lunch

Session 2
13:45 – 15:25 Hash Cryptanalysis

13:45 – 14:10 On Randomizing Hash Functions to Strengthen the Security of Digital Signatures
Praveen Gauravaram, Lars R. Knudsen

14:10 – 14:35 Cryptanalysis of MDC-2
Lars R. Knudsen, Florian Mendel, Christian Rechberger, Soeren S. Thomsen

14:35 – 15:00	Cryptanalysis on HMAC/NMAC-MD5 and MD5-MAC <i>Xiaoyun Wang, Hongbo Yu, Wei Wang, Haina Zhang, Tao Zhan</i>
15:00 – 15:25	Finding Preimages in Full MD5 Faster than Exhaustive Search <i>Yu Sasaki, Kazumaro Aoki</i>
15:25 – 16:25	Coffee Break + Poster Session Slot
Session 3 16:25 – 17:40	Group and Broadcast Encryption
16:25 – 16:50	Asymmetric Group Key Agreement <i>Qianhong Wu, Yi Mu, Willy Susilo, Bo Qin, Josep Domingo-Ferrer</i>
16:50 – 17:15	Adaptive Security in Broadcast Encryption Systems (with Short Ciphertexts) <i>Craig Gentry, Brent Waters</i>
17:15 – 17:40	Traitors Collaborating in Public: Pirates 2.0 <i>Olivier Billet, Duong-Hieu Phan</i>
April 28, 2009 Tuesday	
08:30	Registration Desk open
Session 4 09:00 – 10:15	Cryptosystems I
09:00 – 09:25	Key Agreement from Close Secrets over Unsecured Channels <i>Bhavana Kanukurthi, Leonid Reyzin</i>
09:25 – 09:50	Order-Preserving Symmetric Encryption <i>Alexandra Boldyreva, Nathan Chenette, Younho Lee, Adam O'Neill</i>
09:50 – 10:15	A Double-Piped Mode of Operation for MACs, PRFs and PROs: Security beyond the Birthday Barrier <i>Kan Yasuda</i>
10:15 – 11:10	Coffee Break + Poster Session Slot
Session 5 11:10 – 12:25	Cryptanalysis
11:10 – 11:35	On the Security of Cryptosystems with Quadratic Decryption: The Nicest Cryptanalysis <i>Guilhem Castagnos, Fabien Laguillaumie</i>
11:35 – 12:00	Cube Attacks on Tweakable Black Box Polynomials <i>Itai Dinur, Adi Shamir</i>
12:00 – 12:25	Smashing SQUASH-0 <i>Khaled Ouafi, Serge Vaudenay</i>
12:25 – 13:30	Lunch

Extended Euclidean Algo on Them

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22.4.09

(3)

$15 \in \mathbb{Z}_{87}$ Inverse?

r	q	s	t	
<u>87</u>	.	<u>1</u>	<u>0</u>	$3 \cdot 87 + 1 \cdot 15 = r$
15	5	0	1	$1 \cdot 87 + 0 \cdot 15 = 87$
$(15) - 5 \cdot (15):$	1	1	-5	$0 \cdot 87 + 1 \cdot 15 = 15$
$(15) - 1 \cdot (12):$	4	-1	6	$1 \cdot 87 + (-5) \cdot 15 = 12$
<u>3</u>				$(-1) \cdot 87 + 6 \cdot 15 = 3$
0		5	-29	$5 \cdot 87 + (-29) \cdot 15 = 0 \leftarrow \text{X check!}$

$14 \in \mathbb{Z}_{93}$ Inverse?

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(1)

r	q	s	t	
93		1	0	
14	6	0	1	
8	1	1	-6	
5	1	-1	7	
4	1	2	-13	
1	4	-3	20	$\rightarrow 1 = (-3) \cdot 93 + 20 \cdot 14$
0		14	-93	ic. $1 = (20) \cdot 14$ in \mathbb{Z}_{93}

X check: ok!

$$0 = 14 \cdot 93 + (-93) \cdot 14$$

In our first example we did not ^{28.4.09}
find a solution. But we notice
that 13 divides 87 and 15.

So any combination

$$b \cdot 15 + k \cdot 87$$

is divisible by 3. BUT 1 is not
divisible by 3. So there is no solution!

Then

The Extended Euclidean Algorithm
finds a solution (s, t) of

$$s \cdot a + t \cdot b = 1$$

or produces a non-trivial divisor
of a, b which proves that no solution
exists.

Actually, the last non-zero remainder r
is a (the) greatest common divisor of
 a and b .

Moreover: over \mathbb{Z} the runtime is $O(n^2)$. ^{bitsize of a and b} \square

As a corollary we obtain a description of the invertible elements in \mathbb{Z}_N :

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(3)

$$\begin{aligned}\mathbb{Z}_N^\times &= \{ a \in \mathbb{Z}_N \mid \overbrace{\exists b \in \mathbb{Z}_N: b \cdot a = 1}^{a \text{ is invertible}} \} \\ &= \{ a \in \mathbb{Z}_N \mid \gcd(\underbrace{a}_{\substack{\uparrow \\ \text{greatest common divisor}}}, N) = 1 \}\end{aligned}$$

Chinese Remainder Theorem

Assume $N = m_1 \cdot m_2$,
 $\gcd(m_1, m_2) = 1$.

Then

$$\mathbb{Z}_N \xrightarrow{\cong} \mathbb{Z}_{m_1} \times \mathbb{Z}_{m_2}$$

$$a \mapsto (a \bmod m_1, a \bmod m_2)$$

is an isomorphism!

Consider: $N = 15 = 3 \cdot 5$

$\mathbb{Z}_3 \backslash \mathbb{Z}_5$	0	1	2	3	4
0	0	6	12	3	9
1	10	1	7	13	4
2	5	11	2	8	14

counterexample
 $N = 4 = 2 \cdot 2$

$\mathbb{Z}_2 \backslash \mathbb{Z}_2$	0	1
0	0, 2	?
1	?	1, 3

This works vice by assumption
the gcd of m_1 and m_2 is 1.

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We get

$$\begin{aligned} a &= \check{b} \cdot a_1 + \check{c} \cdot a_2 \\ &= \check{b} \cdot k_2 m_2 + \check{c} \cdot k_1 m_1. \end{aligned}$$

Example Find $a \in \mathbb{Z}_{15}$ such that
 $a \mapsto (2, 2) \in \mathbb{Z}_3 \times \mathbb{Z}_5$.

Run EEA (3, 5) and obtain

$$\underbrace{2 \cdot 3}_{a_2} + \underbrace{(-1) \cdot 5}_{a_1} = 1.$$

$\check{a}_1 \bmod 3 = 1$		$\check{a}_2 \bmod 3 = 0$		2
$\check{a}_1 \bmod 5 = 0$		$\check{a}_2 \bmod 5 = 1$		2
				2 ←

$$a = 2 \cdot ((-1) \cdot 5) + 2 \cdot (2 \cdot 3) = 2.$$

Why don't we stop here?

What's the basic difference

between $(\mathbb{Z}_N, +)$,

(\mathbb{Z}_N, \cdot) ?

Actually, for any finite group G
and any element g ,

there is a number $\ell > 0$ such
that $g^\ell = 1$.

(In $g^0, g^1, g^2, \dots, g^{\ell-1}, \dots$ you find
somewhere twice the same result, i.e.

$\ell_1 > \ell_2 : g^{\ell_1} = g^{\ell_2}$. Since we can divide we have
 $g^{\ell_1 - \ell_2} = 1$.)

And so the map $d \{g^x \mid x \in \mathbb{Z}\}$

$$\begin{array}{ccc} (\mathbb{Z}_\ell, +) & \longrightarrow & \langle g \rangle \subset (G, \cdot) \\ \alpha \text{ mod } \ell & \longrightarrow & g^\alpha \end{array}$$

is a homomorphism and

actually an isomorphism between

$(\mathbb{Z}_\ell, +)$ and $(\langle g \rangle, \cdot)$.

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Compute this?

Silly answer: compute

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(7)

$$g^x = \underbrace{g \cdot g \cdot \dots \cdot g}_{\alpha \text{ of } g}$$

$(\alpha-1)$ operations in G .

But $\alpha \approx 2^n$ where $n = \# \text{bits in } g$,
so the runtime is exponential.

Better: use square & multiply.

Example Compute g^{25} eagerly:

$g^1, g^2, g^4, g^8, g^{16}, g^{24}, g^{25}$

$\underbrace{g^1, g^2, g^4, g^8, g^{16}}_{\text{store}}, g^{24}, g^{25}$

Square as often as possible,
multiply with most latest fitting til done.

runtime: $O(n)$ op's in G .

memory: $O(n)$ elt's in G .

Example compute g^{25} by square & multiply:

$g^1, g^2, g^3, g^6, g^{12}, g^{24}, g^{25}$

$\underbrace{g^1, g^2, g^3}_{\text{store}}, g^6, g^{12}, g^{24}, g^{25}$

time: $O(n)$

space: $3 \in O(1)$

What about finding α
given $a = g^\alpha$?

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⑧

This is called the
Discrete Logarithm Problem.

And: for $(\mathbb{Z}_N, +)$ it's easy,
for $(\mathbb{Z}_N^\times, \cdot)$ it's often probably
difficult.

14:00 – 18:00	<p>Social Program - Meeting Point 13:40 in the foyer!</p> <ul style="list-style-type: none"> • City Walking Tour (2,5 h) • City Bike Tour (3h) • Chocolate Museum (1h) • Wallraf-Richartz Museum (1h) • Boat Cruise (1h)
18:00 – 23:00	Rump Session
April 29, 2009 Wednesday	
09:00 – 9:15	Best Paper Award Ceremony
Session 6 09:15 – 10:30	Cryptosystems II
09:15 – 09:40	Practical Chosen Ciphertext Secure Encryption from Factoring <i>Dennis Hofheinz, Eike Kiltz</i>
09:40 – 10:05	Realizing Hash-and-Sign Signatures under Standard Assumptions <i>Susan Hohenberger, Brent Waters</i>
10:05 – 10:30	A Public Key Encryption Scheme Secure against Key Dependent Chosen Plaintext and Adaptive Chosen Ciphertext Attacks <i>Jan Camenisch, Nishanth Chandran, Victor Shoup</i>
10:30 – 11:25	Coffee Break + Poster Session Slot
Invited Talk 11:25 – 12:25	Cryptography without (Hardly any) Secrets ? <i>Shafi Goldwasser</i>
12:25 – 13:45	Lunch
Session 7 13:45 – 15:25	Security, Proofs and Models II
13:45 – 14:10	Salvaging Merkle-Damgard for Practical Applications <i>Yevgeniy Dodis, Thomas Ristenpart, Thomas Shrimpton</i>
14:10 – 14:35	On the Security of Padding-Based Encryption Schemes (Or: Why we cannot prove OAEP secure in the Standard Model) <i>Eike Kiltz, Krzysztof Pietrzak</i>
14:35 – 15:00	Simulation without the Artificial Abort: Simplified Proof and Improved Concrete Security for Waters' IBE Scheme <i>Mihir Bellare, Thomas Ristenpart</i>
15:00 – 15:25	On the Portability of Generalized Schnorr Proofs <i>Jan Camenisch, Aggelos Kiayias, Moti Yung</i>
15:25 – 15:45	Coffee Break

April 29, 2009 Wednesday

Session 8 15:45 – 16:35	Side Channels
15:45 – 16:10	A Unified Framework for the Analysis of Side-Channel Key Recovery Attacks <i>Francoix-Xavier Standaert, Tal Malkin, Moti Yung</i>
16:10 – 16:35	A Leakage-Resilient Mode of Operation <i>Krzysztof Pietrzak</i>
16:45 – 18:00	IACR Membership Meeting
19:00 – 23:00	Conference Dinner - Boat Cruise (2h, the boat leaves the pier of K&D at 20:00)

April 30, 2009 Thursday

Session 9 09:00 – 10:40	Curves
09:00 – 09:25	ECM on Graphics Cards <i>Daniel Bernstein, Tien-Ren Chen, Chen-Mou Cheng, Tanja Lange, Bo-Yin Yang</i>
09:25 – 09:50	Double-Base Number System for Multi-Scalar Multiplications <i>Christophe Doche, David Kohel, Francesco Sica</i>
09:50 – 10:15	Endomorphisms for Faster Elliptic Curve Cryptography on a Large Class of Curves <i>Steven Galbraith, Xibin Lin, Michael Scott</i>
10:15 – 10:40	Generating Genus Two Hyperelliptic Curves over Large Characteristic Finite Fields <i>Takakazu Satoh</i>
10:40 – 11:10	Coffee Break + Poster Session Slot
Session 10 11:10 – 12:25	Randomness
11:10 – 11:35	Optimal Randomness Extraction from a Diffie-Hellman Element <i>Pierre-Alain Fouque, Sebastien Zimmer, David Pointcheval, Celine Chevalier</i>
11:35 – 12:00	Verifiable Random Functions from Identity-based Key Encapsulation <i>Michel Abdalla, Dario Catalano, Dario Fiore</i>
12:00 – 12:25	A New Randomness Extraction Paradigm for Hybrid Encryption <i>Eike Kiltz, Krzysztof Pietrzak, Martijn Stam, Moti Yung</i>
12:25 – 12:40	Closing Remarks

What about finding α

given $a = g^\alpha$?

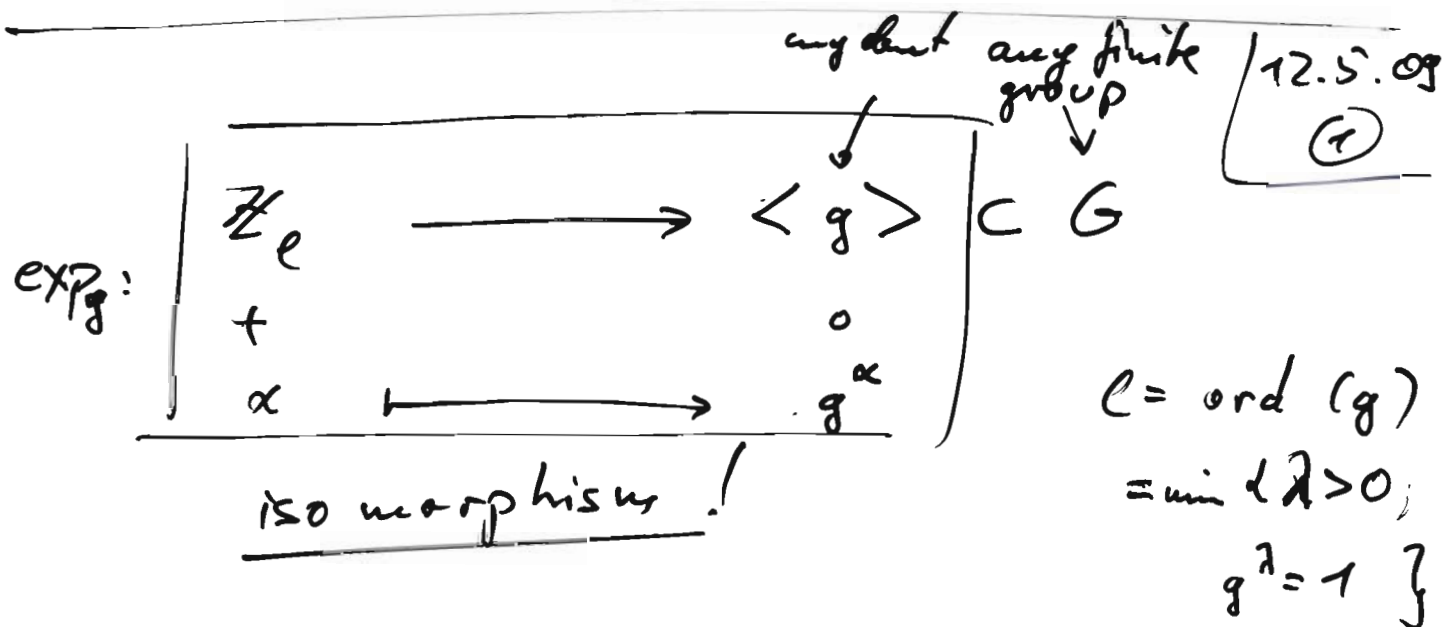
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This is called the

Discrete Logarithm Problem.

And: for $(\mathbb{Z}_N, +)$ it's easy,

for $(\mathbb{Z}_N^\times, \cdot)$ it's often probably
difficult.



Remark note:

It's surjective. Assume you find α, β
with $g^\alpha = g^\beta$. Then $g^{\alpha-\beta} = 1$

But of course $-e < \alpha - \beta < e$, wlog. $0 \leq \alpha - \beta < e$

(otherwise exchange α, β). But $g^\lambda \neq 1$ for $0 < \lambda < e$.

Thus $\alpha = \beta$. That is: exp_g is injective!

Compute the inverse of \exp_g
means to solve a

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②

Discrete Logarithm Problem

Given $a \in \langle g \rangle$
Look for $\alpha \in \mathbb{Z}_e$ s.t. $a = g^\alpha$.

Example

$G = (\mathbb{Z}_N, +)$: DLP solvable
in time $O((\log_2 N)^2)$
using the Extended
Euclidean Algorithm

$G = (\mathbb{Z}_N^\times, \cdot)$:
DLP solvable
in time $O(\sqrt{\ell})$
where ℓ = largest prime factor
of $\# \mathbb{Z}_N^\times$.

Case: $N=p$ prime

$$\# \mathbb{Z}_p^\times = p-1.$$

$\{ a \bmod N \mid \gcd(a, N) = 1 \}$
decide by
EEA!

eg.: $p = 101$, $p-1 = 100 = 2^2 \cdot 5^2$.

Thus there is a DLGG-algorithm
of runtime roughly $\sqrt{51} \ll \sqrt{100}$.

Solution for DLOG in time \sqrt{p} :

Given $g \in G$, of order p .

Given $a \in \langle g \rangle$.

Find $x \in \mathbb{Z}_p$ s.t. $g^x = a$.

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(3)

"Meet in the middle" attack

→ Baby step - giant step.

Choose $b = \sqrt{p}$ (as $b = 2^{\lceil \frac{1}{2} \log_2 p \rceil}$.)

Write $x = x_1 \cdot b + x_0$ with $0 \leq x_1, x_0 < b$.

Thus we have to solve this:

$$(g^b)^{x_1} \cdot g^{x_0} = a$$

$$(g^b)^{x_1} = a \cdot g^{-x_0}.$$

Compute a table with

$$[x_0, a \cdot g^{-x_0}] \text{ for } 0 \leq x_0 < b.$$

then run through possible $0 \leq x_1 < b$

and compute $(g^b)^{x_1} = (g^b)^{x_1-1} \cdot g^b$

and check whether it is in the table.

deterministic
runtime \mathcal{O}

$\mathcal{O}(b) = \mathcal{O}(\sqrt{p})$
operations (& space)

Better:

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(4)

Pollard- ρ

runs in heuristic expected
time $O(\sqrt{e})$
and space $O(1)$.

Compute many
 $g^{\alpha} a^{\beta}$.

If we find a collision i.e.

$$g^{\alpha_1} a^{\beta_1} = g^{\alpha_2} a^{\beta_2}$$

then

$$g^{\alpha_1 - \alpha_2} = a^{\beta_2 - \beta_1}$$

i.e.

$$g^{\frac{\alpha_1 - \alpha_2}{\beta_2 - \beta_1}} = a \quad \text{if } \beta_2 - \beta_1 \in \mathbb{Z}_C^{\times}.$$

We expect to choose $O(\sqrt{e})$ many (α, β)
until we find a collision.

Floyd's trick saves memory!

Fix a function $(\alpha, \beta, g^{\alpha} a^{\beta})$
and maps it to a new one of this form.

Now proceed:

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(5)

Pick $\alpha_0, \beta_0 \in \mathbb{Z}_e$,

compute $g^{\alpha_0} a^{\beta_0} = \cancel{u(x_0)} = y_0$

~~Repeat~~: $x_0 := (\alpha_0, \beta_0, g^{\alpha_0} a^{\beta_0})$,

$y_0 := (\alpha_0, \beta_0, g^{\alpha_0} a^{\beta_0})$.

$i := 1$

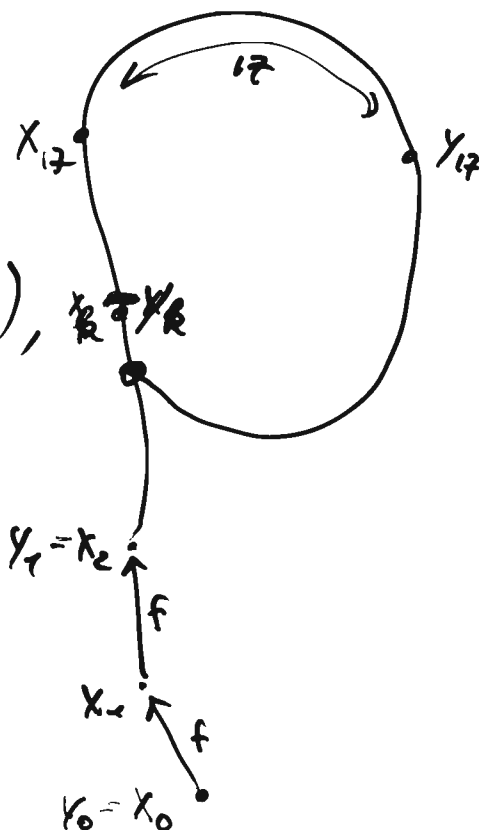
Repeat

$x_i = f(x_{i-1})$,

$y_i = f(f(y_{i-1}))$, ~~$x_i = y_i$~~

$i = i + 1$

until $(x_i)_3 = (y_i)_3$. $y_i = x_i$



We lost the precise analysis,
but in practice it works!

So heuristic expected runtime $O(\sqrt{e})$.

and space $O(1)$

Can we use specific properties
of \mathbb{Z}_N^* to get an even
better algorithm?

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⑥

Yes: $O(\sqrt{\log_2 N} \log_2 \log_2 N)$
runtime 2
(space)

This is subexponential
but not polynomial in $\log_2 N$.

Actually, we can use
that elements in \mathbb{Z}_N^*
come from integers in \mathbb{Z}
which have a unique prime factorization!

For practical situations we want
that the runtime of any known
attack is large.

This leads to $\log_2 N \approx \frac{2048}{(3072)}$
to ensure runtime $\approx 2^{128}$
128-bit security.

So \mathbb{Z}_p^* is ok,

but maybe there's sth better?

Remember: DLP can be solved
in time $O(\sqrt{e})$

if $e = \text{ord}(g)$ prime.

for any group.

As just seen: within $G = \mathbb{Z}_p^*$ we can
do faster.

Q: Are there groups where we can
not do faster?

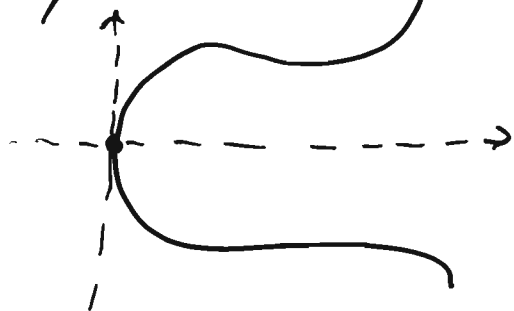
Answer: Probably, yes!

Elliptic Curves

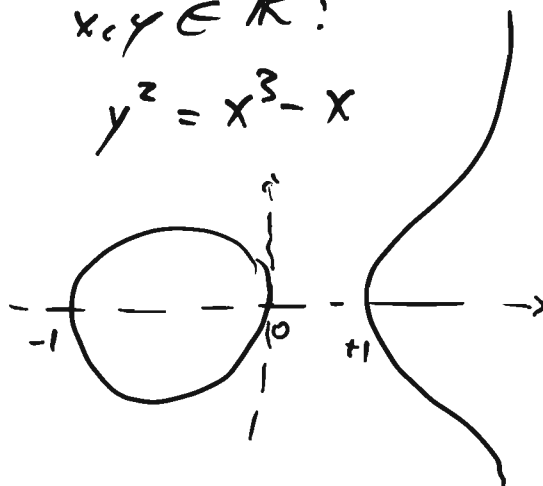
An elliptic curve is (most of the time) given
by an equation $y^2 = x^3 + ax + b$
where $x, y \in \mathbb{F}_p$ with p prime.

To get a feeling consider $x, y \in \mathbb{R}$:

$$y^2 = x^3 + x$$



$$y^2 = x^3 - x$$



Group structure?

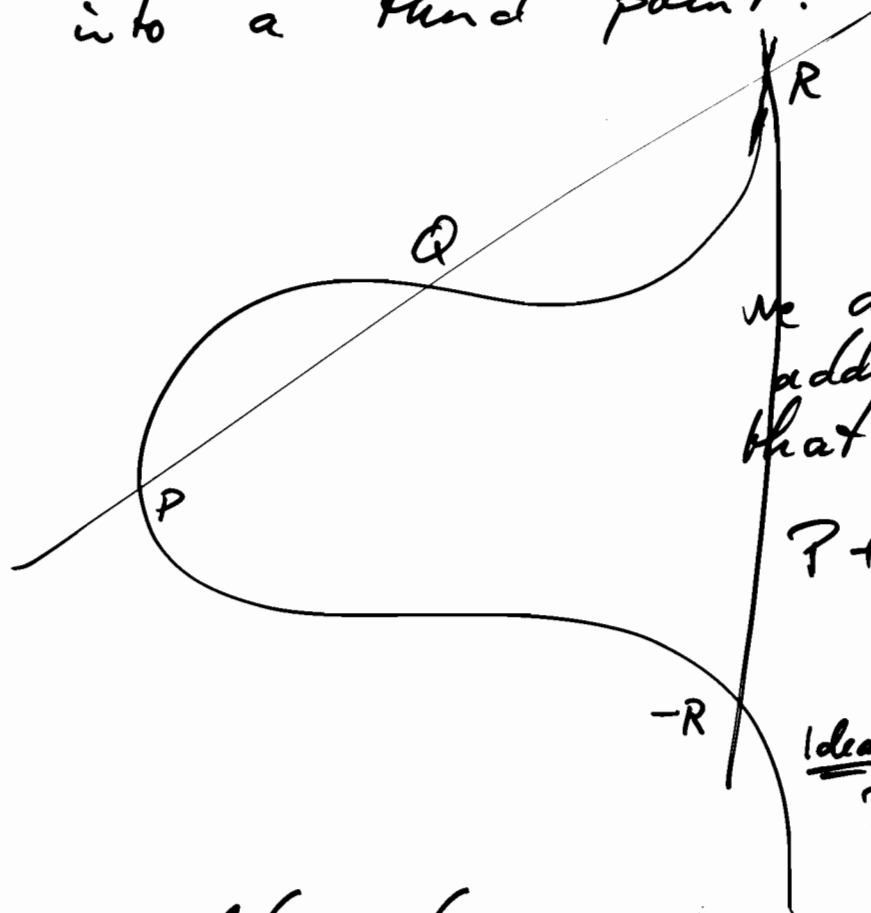
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Basic observation:

it's a degree 3 curve

ie. any line intersects the curve ~~at~~ in (at most) three points.

We would to combine two points into a third point.



We define the addition such that

$$P + Q + R = O.$$

Idea $\left\{ \begin{array}{l} P + Q := -R \end{array} \right.$

We would need now to define $R \mapsto -R$.

Notice: $R \mapsto -R \mapsto +R = R$.

Vertical lines intersect only twice.
(Remember: $y^2 = x^3 + ax + b$.)

We add a point O at infinity lying on any vertical line. Then $R + (-R) = -O = O$.

Formulas for the group operation:

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(7)

(1) Negation

$$R = (x_3, y_3) \quad y_3^2 = x_3^3 + ax_3 + b$$

$$\text{then } -R = (x_3, -y_3)$$

Then $R, -R$ lie on the same vertical line and both on the curve.

$$\text{Obviously } -(-R) = R.$$

(2) Addition of different points P, Q ,
where $P \neq -Q, P \neq O \neq Q$

$$P = (x_1, y_1), \quad Q = (x_2, y_2)$$

$$l_{P,Q} : y = \alpha x + \beta$$

$$\text{we find } \alpha = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{which is nice}$$

nice by assumption
 $x_1 \neq x_2$.

$$\text{and } \beta = y_1 - \alpha x_1.$$

So we find for the third point R on $l_{P,Q}$ and the curve E :
 (x_3, y_3)

$$y_3^2 = x_3^3 + ax_3 + b$$

$$y_3 = \alpha x_3 + \beta$$

$$\text{Thus } P(x_3) = -(\alpha x_3 + \beta)^2 + (x_3^3 + ax_3 + b) = 0$$

We already know two solutions
for this equation: x_1, x_2 .

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Thus can compute

$$P(x) = \underbrace{(x - x_1)(x - x_2)}_{+0} = (x - \cancel{x_3}).$$

ie.

the x^2 -coefficient of P
must be $-(x_1 + x_2 + x_3)$.

On the other hand // it is by def. of P :
 $-\alpha^2$

Thus

$$x_3 = \alpha^2 - x_1 - x_2.$$

and

$$y_3 = \alpha x_3 + \beta = \alpha(x_3 - x_1) + y_1$$

Thus if we let $P + Q = (x_4, y_4)$,

$$\alpha = \frac{y_2 - y_1}{x_2 - x_1},$$

then

$$x_4 = \alpha^2 - x_1 - x_2,$$

$$y_4 = -y_1 + \alpha(x_1 - x_4).$$

(2b) Addition of P with itself, $P \neq O$.
 \rightarrow use tangent: $\alpha = \frac{3x_1^2 + a}{2y_1}.$

Everything else is as above.

(2c) Addition of P and $Q = -P \neq O$ cpb
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③

$$P + (-P) = O$$

(2d) Addition of P and O

$$P + O = P$$

$$O + P = P$$

$$O + O = O$$

Now we have

(P) { a set $E = \{ (x, y) \in \mathbb{F}^2 \mid y^2 = x^3 + ax + b \}$
 $\cup \{ O \}$
 and
 a negation $- : E \rightarrow E$
 $P \mapsto -P$
 $O \mapsto O$
 and
 an addition $+ : E \times E \rightarrow E$
 $(P, Q) \mapsto P + Q$.
 and
 a neutral element: $O \in E$.

A: defer ...

N: O is neutral by definition.

I: $P + (-P) = O$.

C: inspect the definition: $P + Q = Q + P$.

Associativity?

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④

Tricky.

- Historical: Divisors, Picard-group and Riemann-Roch. \ddots

- Geometrical: Possible, but... cumbersome.

- Algebraically?

$$\text{Fix } P = (x_1, y_1),$$

$$Q = (x_2, y_2),$$

$$R = (x_3, y_3)$$

non-special!

$$P \neq \pm Q$$

$$Q \neq \pm R$$

$$P+Q \neq \pm R$$

$$Q+R \neq \pm P$$

Find a formula for

$$(P+Q)+R$$

and

$$P+(Q+R)$$

and compare the formulas.

Not really satisfying.

But it works!

Our goal is:
construct groups with
a point of
known order.

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①

In particular, we should be able to
compute the size of the group.

$$\# \mathbb{Z}_N^+ = N$$

$$\# \mathbb{Z}_p^* = p - 1 \quad (\text{assuming } p \text{ prime})$$

$$\# E_{a,b} = ? \quad (a, b \in \mathbb{F}_q)$$

$$\{(x, y) \in \mathbb{F}_q^2 \mid y^2 = x^3 + ax + b\} \cup \{O\}$$

↑ # of elements in the field

(Side remark: for every prime power q
there exists essentially one field
with q elements. If p is prime,
the $\mathbb{F}_p = \mathbb{Z}_p$.)

Count ver 0: Try all pairs $(x, y) \in \mathbb{F}_q$
 $O(q^2)$ and check if $y^2 = x^3 + ax + b$.
output count if true.

Count ver 1: Try all values $x \in \mathbb{F}_p$,
and decide whether
2.1.0 solutions exists
with $y^2 = x^3 + ax + b$.

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(2)

If you can: take square root
of the $x^3 + ax + b$.

1 solution $\Leftrightarrow \Delta \neq 0$.

$O(p)$

Deciding whether $x^3 + ax + b$
is a square modulo p
can be done in time $O(n^2)$
where $n = \text{bitlength}(p)$.

↑ Jacobi symbol:

$$\left(\frac{c}{d}\right) = \prod_i \left(\frac{c}{d_i}\right)^{e_i}$$

$d = d_i^{e_i}$, d_i are all prime

$$\text{and } \left(\frac{c}{p}\right) = \begin{cases} +1 & \text{if } c \text{ square mod } p \\ 0 & \text{if } c = 0 \\ -1 & \text{if } c \text{ non-square} \end{cases}$$

Cool thing:

$$\left(\frac{c}{d}\right) = \left(\frac{c \bmod d}{d}\right)$$

$$= (-1)^{\dots} \left(\frac{d}{c}\right).$$

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③

$$= (-1)^{\dots} \left(\frac{d \bmod c}{c} \right)$$

until $\left(\frac{2}{p} \right) = \dots, \left(\frac{-1}{p} \right) = \dots$

NOTE: This is very similar to the Euclidean algorithm.
 \rightarrow same runtime. \downarrow

In particular, we learn that

$$\# E_{a,b} \leq 2q + 1.$$

Hasse proves much more:

$$\# E_{a,b} = q + 1 - t$$

where $|t| \leq 2\sqrt{q}.$

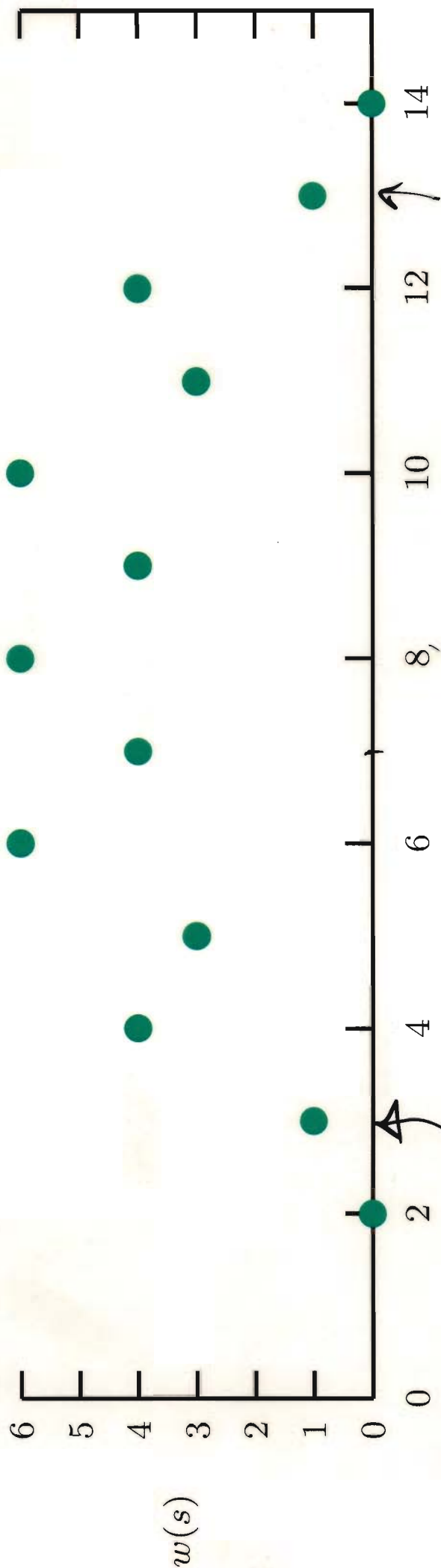
Extra observation: for every curve $E_{a,b}$

there is another one $E_{c,d}$ such that

$$\# E_{a,b} = q + 1 - t, \quad \# E_{c,d} = q + 1 + t.$$

$$\lfloor 2\sqrt{7} \rfloor = 5$$

$$p=q=7$$



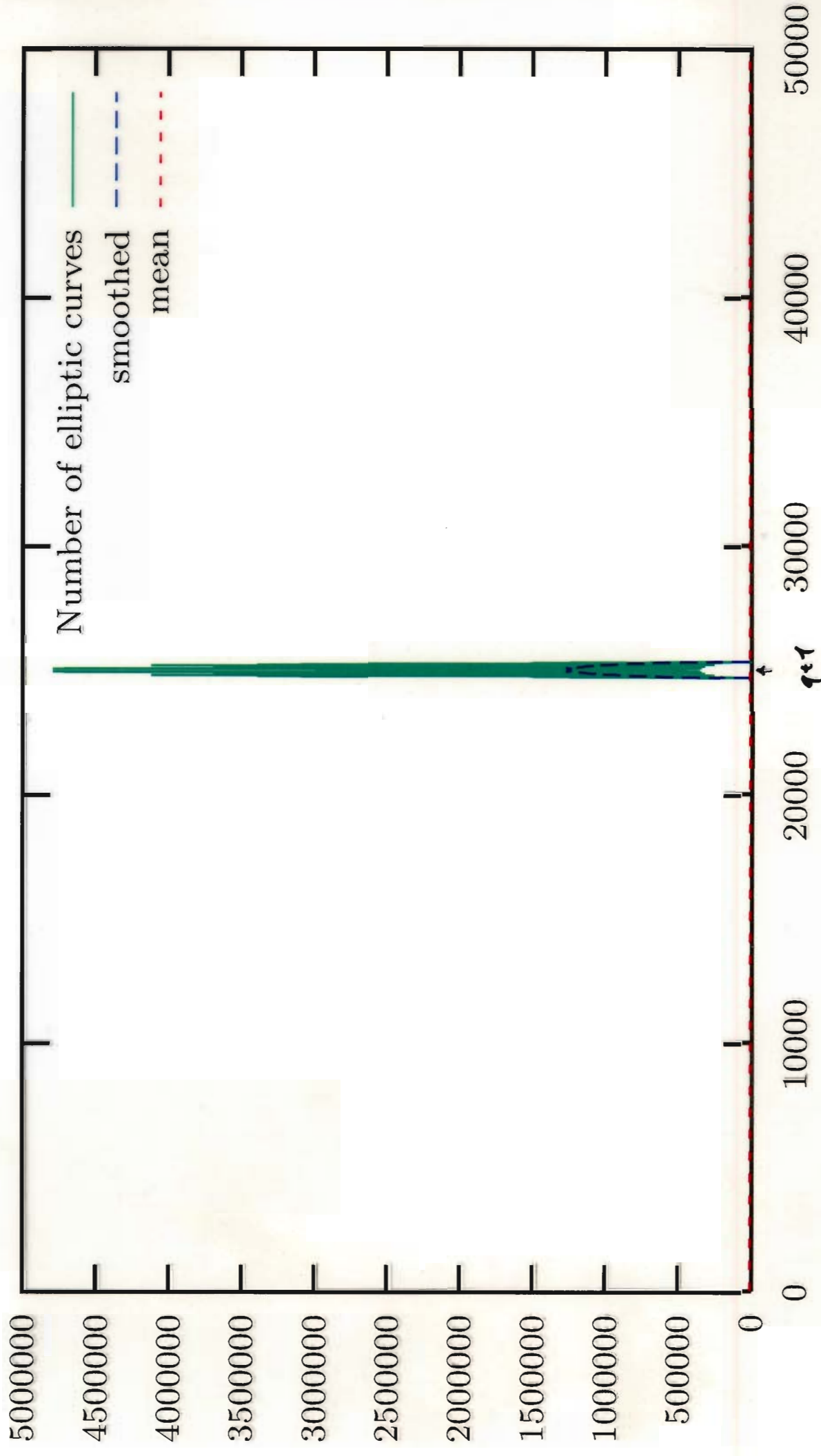
s

$q+1$

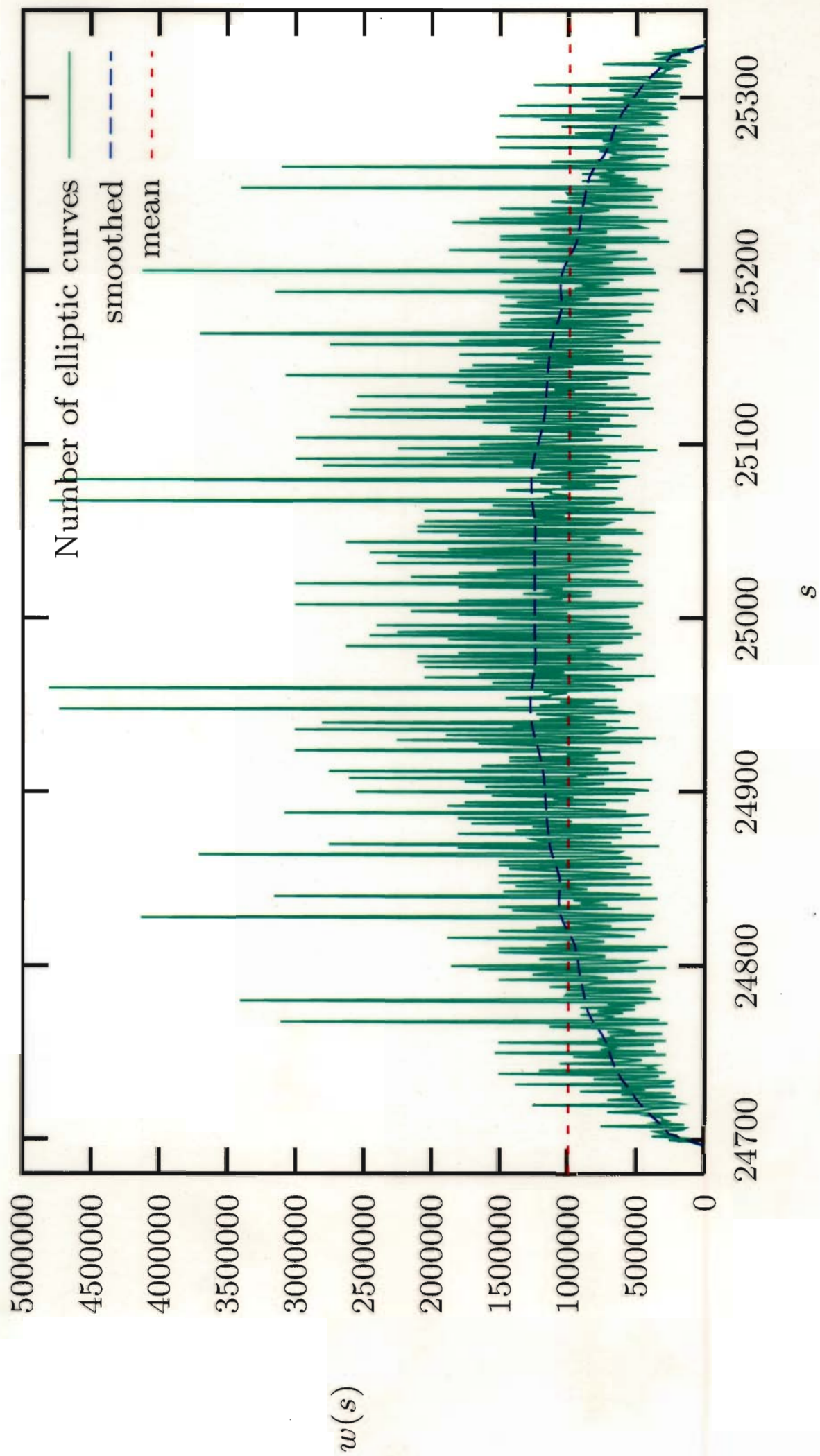
$q+1+5$

$q+1-5$

$p = q = 28013$. # curves



2941.



So we have a way of
computing $\#E_{a,b}$
in time

$$O(q \cdot n^2)$$

$$2^n$$

1

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(24)

~~Schoof~~: pre-Schoof:

Then (Lagrange) G group, finite.

Then for any $a \in G$ we have $a^{\#G} = 1$.
In particular, $\text{ord}(a) \mid \#G$.

Pf of the "in particular":

We know that $a^{\text{ord}(a)} = 1$, $a^{\#G} = 1$.

Use the EEA to ~~write~~ compute

$$g = s \cdot \text{ord}(a) + t \cdot \#G$$

with $g = \gcd(\text{ord}(a), \#G) \leq \text{ord}(a)$.

Now:

$$a^g = \underbrace{(a^{\text{ord}(a)})^s}_{=1} \cdot \underbrace{(a^{\#G})^t}_{=1} = 1.$$

Since $g > 1$, $g \leq \text{ord}(a)$, only $g = \text{ord}(a)$
is possible of the order.

□

So just guess a point P on E . cpb
19.5.03
(5)
Compute $\alpha \cdot P$ for

$$\alpha \in q+1-2\sqrt{q} \dots q+1+2\sqrt{q}.$$

running time: $O(\sqrt{q} \cdot n^3)$

$\approx 2^{4/2}$

still exponential!

Schoof:

Try to determine
 $x^2 \pmod{\ell}$
for some prime ℓ .

That is possible! and in time
 $\text{poly}(n)$,

Do this for $O(n)$ many primes

so that $\ell \geq 4\sqrt{q}$

and then plug things into the

help of the Chinese remainder theorem.

Lake, Elkies and Atkin did many improvements.

SEA
 $O(n^8)$

we will usually need
a group G and
a point $g \in G$ of known order.

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19.3.05
⑥

If $G = E$ with $\#E = \text{prime}$
then just pick any point $P \in E \setminus \{O\}$.

Good news:

for the DLP on a 'random' elliptic
curve nothing better but the generic
algorithms are known.

So: choose $q \approx 256\text{-bit}$,
choose $a, b \in \mathbb{F}_q$,
compute $\#E_{a,b}$
eventually repeat until that is prime
pick $P \in E_{a,b} \setminus \{O\}$.

This will give us 128-bit security (unless...)

Actually, in the verification we have a = public key
 b, r = signature
 m = message.

A first crypto algorithm:

Pick G and $g \in G$ of known order e .

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⑦

Aim: agree on a common key
Diffie-Hellman key agreement

Aline

$$\alpha \in_{\mathbb{R}} \mathbb{Z}_e.$$

$$a = g^{\alpha}$$

Boris

$$\beta \in_{\mathbb{R}} \mathbb{Z}_e.$$

$$b = g^{\beta}$$



$$k_1 = b^{\alpha}$$

$$k_2 = a^{\beta}$$

Observation: $k_1 = k_2$.

$$k_1 = b^{\alpha} = (g^{\beta})^{\alpha} = g^{\beta \cdot \alpha}$$

$$k_2 = a^{\beta} = (g^{\alpha})^{\beta} = g^{\alpha \cdot \beta}$$

Eavesdropper: has g, a, b
wants k .

$$(g, g^{\alpha}, g^{\beta}) \mapsto g^{\alpha\beta}.$$

Diffie-Hellman-Problem (DHP) in G

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(8)

$$(g, g^{\alpha}, g^{\beta}) \longmapsto g^{\alpha\beta}$$

Obviously:

If Eve can solve DLP in G
then she can solve DHP in G .

The other direction is open ... almost!

Thus DH is insecure
if DLP is easy.

We would like to have

if ... is difficult then DH is secure

DHP ✓

DLP?

(No) itam in the middle attack

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①

Alice

$$\alpha \in \mathbb{Z}_e$$

$$a = g^\alpha$$

(Eve)

Wilma

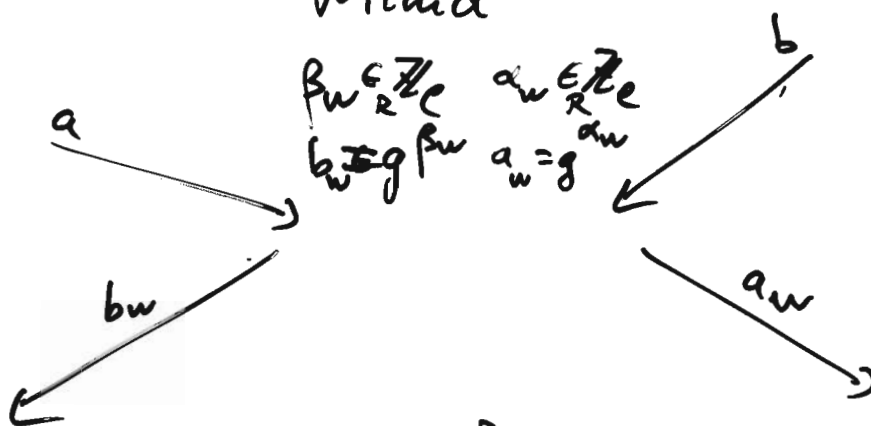
$$\beta_w \in \mathbb{Z}_e \quad \alpha_w \in \mathbb{Z}_e$$

$$b_w = g^{\beta_w} \quad a_w = g^{\alpha_w}$$

Boris

$$\beta \in \mathbb{Z}_e$$

$$b = g^\beta$$



$$k_1 = b_w^\alpha$$

$$= g^{\alpha \beta_w}$$

$$k_{3,w} = a^{\beta_w}$$

$$= g^{\alpha \beta_w} = k_1$$

$$k_2 = a_w^\beta$$

$$= g^{\alpha_w \beta}$$

$$k_{1,w} = b^{\alpha_w}$$

$$= g^{\alpha_w \beta} = k_2$$

Now, Wilma acting as a proxy
can read and manipulate
every thing.



Authenticated key exchange

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(2)

Alice

Boris

$$\alpha \in \mathbb{Z}_p$$

$$a = g^\alpha$$

$$\xrightarrow{a}$$

$$\beta \in \mathbb{Z}_p$$

$$b = g^\beta$$

$$\xleftarrow{b}$$

$$\text{sign}_A(a, b) = \sigma_A$$

$$\xrightarrow{\sigma_A}$$

$$\text{check}((a, b), \sigma_A) = \text{valid!}$$

$$\text{sign}_B(b, a, \sigma_A) = \sigma_B$$

$$\xleftarrow{\sigma_B}$$

$$\text{check}(b, a, \sigma_A, \sigma_B) = \text{valid!}$$

Now, Wilma cannot play
the previous attack!

∴

El Gamal type signatures

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(3)

$$a^{b^*} b^x = g^{\text{hash}(m)}$$

verification equation.

We now have groups where $a, b, g \in G$ can live. And we can make sure that the DLP is reasonably difficult (unless...). Assume further that $\#G$ is prime. Actually, we always require $a, b, g \in \langle g \rangle$. So where does x live?

$$x \in \mathbb{Z}_\ell \quad \text{where} \quad \ell = \text{ord } g.$$

Next: $m \in ? \mathbb{Z}_\ell!$

But $\ell \approx 256$ -bits

Most messages do not fit in

256 bits. \rightarrow Either enlarge the group. I
or: compress the message?

So no, we only need

$$\text{hash}(m) \in \mathbb{Z}_\ell.$$

We cannot

raise a group element a

to the power of a group element b

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So we have to replace the exponent there!

Instead of

$$a^b$$

we put

$$a^{b^*}$$

To ^{any} the ElGamal type signature scheme
first

Setup:

Choose a group G

and an element g

of ~~test prime, but certain~~
known order l .

Make sure that the DLP to the
basis g can be difficult.

(In particular, l must contain
a large prime factor.)

Fix a hash function

$$\text{hash: } \{0, 1\}^* \longrightarrow \mathbb{Z}_l.$$

Choose a simple, easy to
compute function

pb
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5

$$*: G \longrightarrow \mathbb{Z}_e.$$

Examples:

① $G = \mathbb{Z}_p^*$, $g \in G$ of order $e = p-1$.

→ ElGamal signatures.

② $G = \mathbb{Z}_p^*$, $g \in G$ of order $e \mid p-1$
where $p \approx 3072$ Bits, \uparrow prime!

$e \approx 256$ Bits.

→ → DSA (Digital Signature
Algorithm)

③ $G = E_{a,b}$ elliptic curve give by $a, b \in \mathbb{F}_q$.

$P \in G$ of order $e \mid \#E_{a,b}$
 \uparrow prime!

where $q \approx 256$ bits

$e \approx 256$ bits

→ → EC DSA (Elliptic Curve
Digital Signature Algorithm)

ALGORITHMUS. SHA-1.

Eingabe: Eine Nachricht $x \in \{0, 1\}^*$.

Ausgabe: Ein Hashwert $H \in \{0, 1\}^{160}$.

(i) only 80-bit security
(ii) broken.

Konstanten und Rundenfunktionen:

1. $h \leftarrow (67452301, \text{EFCDA}89, 98\text{BADCFE}, 10325476, \text{C3D2E1F0})$.

$$K_j \leftarrow \begin{cases} 5\text{A}827999, & 0 \leq j < 20, & (32 \text{ Bits von } \sqrt{2}) \\ 6\text{E}9\text{D9EBA}1, & 20 \leq j < 40, & (32 \text{ Bits von } \sqrt{3}) \\ 8\text{F}1\text{BBCDC}, & 40 \leq j < 60, & (32 \text{ Bits von } \sqrt{5}) \\ \text{CA}62\text{C1D6}, & 60 \leq j < 80. & (32 \text{ Bits von } \sqrt{7}) \end{cases}$$

$$f_j(B, C, D) = \begin{cases} (B \wedge C) \vee (\bar{B} \wedge D), & 0 \leq j < 20, \\ B \oplus C \oplus D, & 20 \leq j < 40, \\ (B \wedge C) \vee (C \wedge D) \vee (D \wedge B), & 40 \leq j < 60, \\ B \oplus C \oplus D, & 60 \leq j < 80. \end{cases}$$

Vorberechnungen:

2. Auffüllen: $\tilde{x} \leftarrow x | 1 | 0^d | \langle |x| \rangle_{64}$ mit $0 \leq d < 512$ so, daß $|\tilde{x}|$ ein Vielfaches von $512 = 16 \cdot 32$ ist.

3. Zerlege \tilde{x} in 32-Bitworte: $\tilde{x} = x_0 x_1 x_2 \dots x_{16m-1}$.

4. Initialisiere: $(H_1, H_2, H_3, H_4, H_5) \leftarrow h$.

Hauptberechnung:

5. For $i = 0..m - 1$ do 6-13

6. For $j = 0..15$ do $W_j \leftarrow x_{16i+j}$.

7. For $j = 16..79$ do

8. $W_j \leftarrow (W_{j-3} \oplus W_{j-8} \oplus W_{j-14} \oplus W_{j-16}) \oplus 1$.

9. $(A, B, C, D, E) \leftarrow (H_1, H_2, H_3, H_4, H_5)$.

10. For $j = 0..79$ do 11-12

11. $t \leftarrow A \oplus 5 + f_j(B, C, D) + E + W_j + K_j$.

12. $(A, B, C, D, E) \leftarrow (t, A, B \oplus 30, C, D)$.

13. $(H_1, \mathbf{H_2}, \mathbf{H_3}, H_4, H_5) \leftarrow$

$(H_1 + A, H_2 + B, H_3 + C, H_4 + D, H_5 + E)$.

14. Antworte $H_1 | H_2 | H_3 | H_4 | H_5$.

In the verification we have:

	bits	①	②	③
the message	m			
the public key	a			
the signature	b, r	6144	3328	512

Back to the scheme

26.5.09

①

Verification:

Input: a public key $a \in G$
 a message $m \in \{0,1\}^*$
 a signature $b, r \in G \times \mathbb{Z}_\ell$.

1. Return $\left(a b^* b^r = g^{\text{hash}(m)} \text{ in } G \right)$

where $G = \langle g \rangle$, and $g = \ell$.

Setup: Input: security parameter

Output: G a group,
 $g \in G$ element,
 $\ell = \text{ord}(g)$.

User-setup: Input: G, g, ℓ .

Output: $a \in G, \alpha \in \mathbb{Z}_\ell$

Choose $\alpha \in_R \mathbb{Z}_\ell$.

$a := g^\alpha$

Return (a, α)

How to 'solve' the verification equation for (b, y) ?

CP6
26.05.09
(2)

...

Most things are already powers of g ,
with exponents known to the signer...
not yet b but we can choose it
as a power:

Signing

Input: a message m
a secret key α
global setup G, g, e .

1. Choose $\beta \in_R \mathbb{Z}_e$, and
compute $b := g^\beta$

2. Find $y \in \mathbb{Z}_e$ as the (a) solution of
$$\alpha b^* + \beta y = \text{hash}(m) \text{ in } \mathbb{Z}_e$$

for y .

3. Return (b, y) .

CORRECT?

Then of course $b^* y$
ie. it is a signature!
$$= g^{\alpha b^* + \beta y} = g^{\text{hash}(m)}$$

EFFICIENT?

(Ex)

CP 6
26.5.09
(3)

SECURITY?

Let's play a little...

The attacker tries to solve the verification equation w/o the secret key.

First try:

1. Choose any msg m .
2. Choose any b , if you want as $b = g^{\beta}$.
3. Compute the algo

$$b^x = g^{\text{hash}(m)} a^{-b^x} \quad \text{?}$$

- 3', Compute the algo and the ...

$$a = b^x \quad \text{?}$$

Second try

1. Choose m .
2. Choose x .
3. Solve

$$a^{b^x} b^x = g^{\text{hash}(m)} \quad \text{?}$$

Last try

Last try

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(4)

1. Force hash = id.

2. Then there are
nice formula
in same parameters

a

b = f(---)

g = g(---)

m = h(---)

This construct an **EXISTENTIAL
FORGERY.**

However, this attacker has
no way to influence
which message is signed.

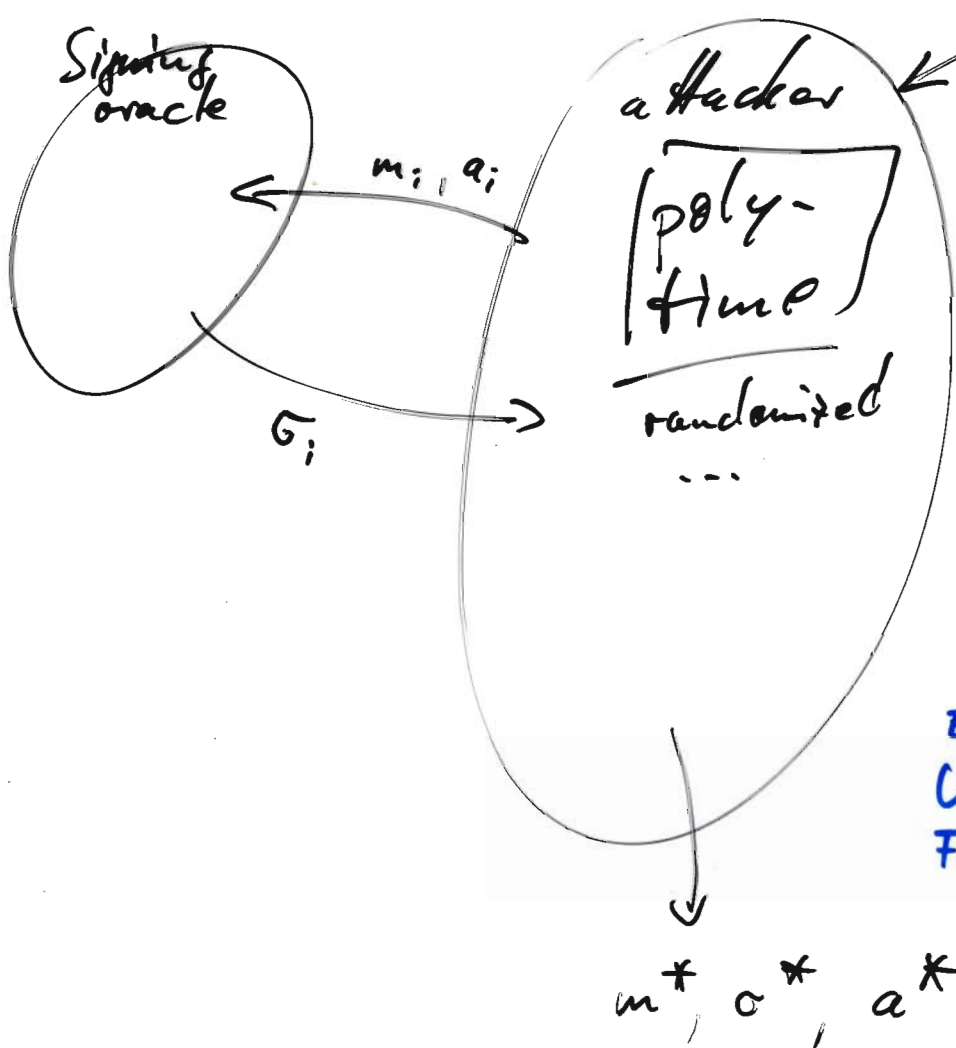
All this is digging in the fog...

Security model

Global setup
G, g, & hash, *

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5

Public keys



EF

EUF - CMA

Existential
Universal
Forgery

Chosen
Message
Attacks

Aim of the attacker:

$$\text{Ver}_{a^*}(m^*, \sigma^*) = \text{TRUE}$$

& (m^*, a^*) never queried.

The attacker wins if his success probability is significantly larger than guessing.

SECURITY

GOAL:

No such
attacker
exists

ECDSA Setup:

- Implement an elliptic curve E (so we can add and subtract points, multiply points with an integer) and choose a point P of prime order q . (In fact, we work in the q -element group $\langle P \rangle$ generated by P .) We assume that q is a, say, 160-bit prime.
- Fix a cryptographic hash function HASH. The DSS chooses SHA-1 which produces a 160-bit value.
- Alice chooses a secret key $\alpha \in_{\mathbb{R}} \mathbb{Z}_q$ and publishes her public key $A = \alpha \cdot P \in E$.

ALGORITHM. ECDSA sign.

Input: Global parameters: the base point P , Alice's public key A , her secret key α and a message $m \in \{0, 1\}^*$.

Output: A signature $(b^*, c) \in \mathbb{Z}_q$.

1. Calculate $e = \text{HASH}(m) \in \mathbb{Z}_q$.
2. Repeat 3–5
3. Choose $\beta \in_{\mathbb{R}} \mathbb{Z}_q^\times$ at random.
4. Calculate $\beta \cdot P = (x_1, y_1)$ in the elliptic curve E and let $b^* = x_1 \bmod q$.
5. Solve $\beta c = e + \alpha b^*$ in \mathbb{Z}_q for $c \in \mathbb{Z}_q$.
6. Until $b^* \neq 0$ and $c \neq 0$
7. Return (b^*, c) .

ALGORITHM. ECDSA verify.

Input: Global parameters: the base point P , Alice's public key A , the message $m \in \{0, 1\}^*$ and the signature $(b^*, c) \in \mathbb{Z}_q \times \mathbb{Z}_q$.

Output: A boolean value stating whether the signature is valid.

1. Verify that $b^*, c \in \mathbb{Z}_q$. Else Return FALSE.
2. Calculate $e = \text{HASH}(m) \in \mathbb{Z}_q$.
3. Calculate $(x_1, y_1) = c^{-1}e \cdot P + c^{-1}b^* \cdot A \in E$.
4. If $x_1 \bmod q \neq b^*$ then Return FALSE
5. Else Return TRUE

If both parties are honest then

$$\begin{aligned} c^{-1}e \cdot P + c^{-1}b^* \cdot A &= c^{-1}(e + b^* \alpha) \cdot P \\ &= c^{-1}\beta c \cdot P = \beta \cdot P \end{aligned}$$

and so the x -coordinate of this point is the same that was used to define b^* and the signature is valid.

SECURITY REDUCTION

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26.5.09

⑥

Prove a statement like:

If Problem X is difficult

then our scheme is EUF-CMA-secure.

We won't do anything like here...

CONSEQUENCES?

statements like

If our scheme is ...-secure
then ... the hash-function used
has property A .

Then

If ECDSA signatures for $(G, g, P, \mathbb{Z}, \text{hash})$
are secure

then the DLP for $g \in G$
must be difficult.

Proof

Construct an attacker!

Eg. 1. Compute α from a by the DLP subroutine.
2. Generate signature...

Thm If ElGamal type signatures
for $(G, g, e, *, \text{hash})$ are secure
the the hash function hash
is collision-resistant.

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28.5.03
(7)

Def A hash function family $(\{0, 1\}^* \rightarrow \{0, 1\}^k)_k$
is collision-resistant
if it is difficult to find

$$x, y \in \{0, 1\}^*,$$

$$x \neq y,$$

$$\text{hash}(x) = \text{hash}(y).$$

↑ ~~difficult~~ = poly time and significant
not difficult success prob.

Proof Assume that the attacker has an efficient
subroutine that often can produce collisions
for the hash function.

1. Call this subroutine and get $m_1 \neq m_2$,
 $\text{hash}(m_1) = \text{hash}(m_2)$.
2. Call the signing oracle on m_1 and obtain σ_1 .
3. Output (m_2, σ_1) .

□

Then If ElGamal type signatures
for $(G, g, p, H, \text{hash})$ are secure
~~secure~~

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⑧

the the hash function
is one-way.

one-way = difficult to find
preimages

Proof (Ex)

]

ElGamal type \rightarrow DSA

change verification so that
only b^* is needed!

We had $a^{b^*} [b]^r = g^{\text{hash}(m)}$

Solve for this position

$$b = b^r = b^{rr^{-1}} = \left(g^{\text{hash}(m)} a^{b^*} \right)^{r^{-1}}$$

in the
 \approx

thus

$$b^* = \left[\left(g^{\text{hash}(m)} a^{b^*} \right)^{r^{-1}} \right]^*$$

Use this as verification! \rightarrow Save size
in signatures.

MRTDs as described/required
by ICAO

cpb
18.5.09
①

1. based on RFID technology

→ consequence that one can
communicate with the chip
from distances of up to 1.5m
(or 10m with special equipment)

Problem: data on the chip is sensitive
and must not be leaked
out

(a) unless the reader
physically accesses to
the MRTD

machine
readable
travel document.

and

(b) unless the reader
is authorized to
read.

side remarks:

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105.09
②

RFID = radio frequency
identification

two variants:

① without power supply or battery

• with battery

↓
short lifetime
& long distance
(~100m)

↓
long lifetime
& short distance

Basic Access Control

- MUST use the information written in the machine readable zone (MRZ) to produce some keying material
- all further communication MUST be secured with "secure messaging" i.e. encryption & authentication

Passive Authentication

- chip has to verify a certificate given by the reader. This certificate is a signed electronic document containing
 - access rights

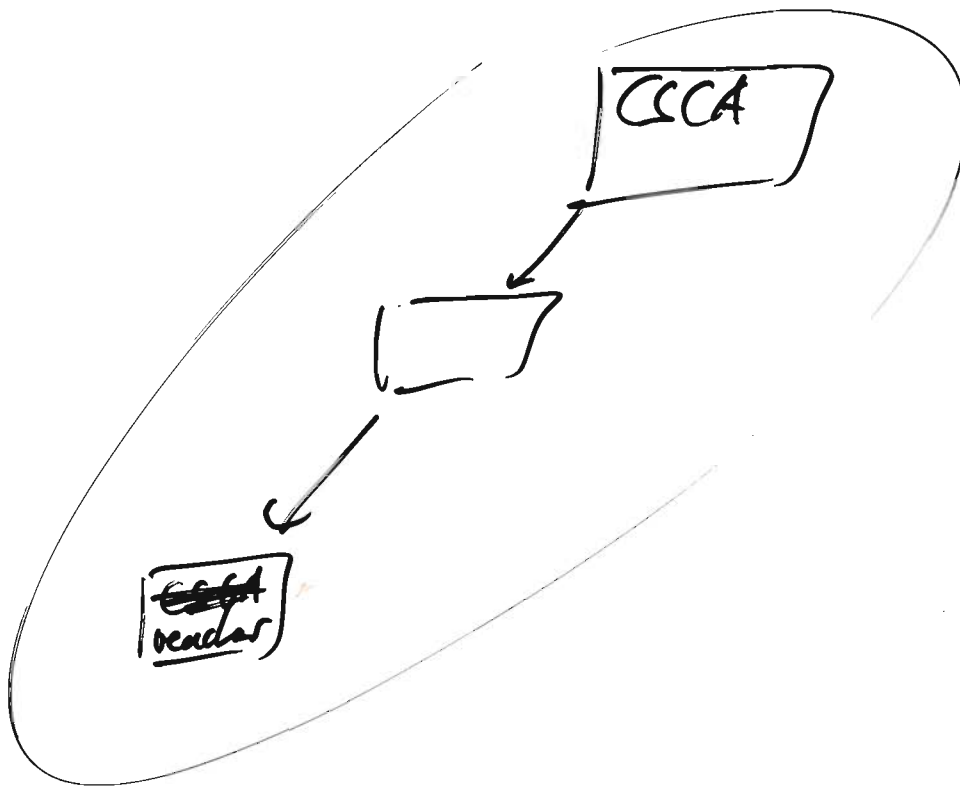
- o id information
- o public key
- o signature of
as higher authority

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(3)

The chip ~~knows~~ has the

- o Country Signing CA certificate
contains similar info.
public key : 3072 bit RSA key, or
256 bit EC key

For complete verification the chip
needs the certificate chain up to
the country signing CA.



- o Document Signer CA certificate
with CSCA signature
(2048 bit RSA key or 224 bit EC key)

Active Authentication

- visual access to MRZ in order to do the basic access control.

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10.509
(4)

Extended Access Control (OPTIONAL)

- to protect information like finger prints which is not found in the non-electronic part of the MRTD.
- biometrics may be additionally encrypted! [e.g. Diffie-Hellman]

BAC

- (i) inspection of the MRZ
MRZ-information \leftarrow Document Number ||
Date-of-birth ||
Date-of-expiry
- (ii) derive keys from this
- (iii) authentication & key establishment
- (iv) ~~after~~ after that use the established keys for secure messaging

Technical Report

PKI for Machine Readable Travel Documents offering ICC read-only access

Release : 1.1

Date : October 01, 2004

Annex E Basic Access Control and Secure Messaging

E.1 Key Derivation Mechanism

The computation of 2 key 3DES keys from a key seed (K_{seed}) is used in both the establishment of the Document Basic Access Keys (K_{ENC} and K_{MAC}) and the establishment of the Session keys for Secure Messaging.

A 32 bit counter c is used to allow for deriving multiple keys from a single seed. Depending on whether a key is used for encryption or MAC computation the following values MUST be used:

- $c = 1$ (i.e. '0x 00 00 00 01') for encryption.
- $c = 2$ (i.e. '0x 00 00 00 02') for MAC computation.

The following steps are performed to derive 2 key 3DES keys from the seed K_{seed} and c :

1. Let D be the concatenation of K_{seed} and c ($D = K_{seed} || c$).
2. Calculate $H = \text{SHA-1}(D)$ the SHA-1 hash of D .
3. Bytes 1..8 of H form key K_a and bytes 9..16 of H form key K_b .
4. Adjust the parity bits of keys K_a and K_b to form correct DES keys.

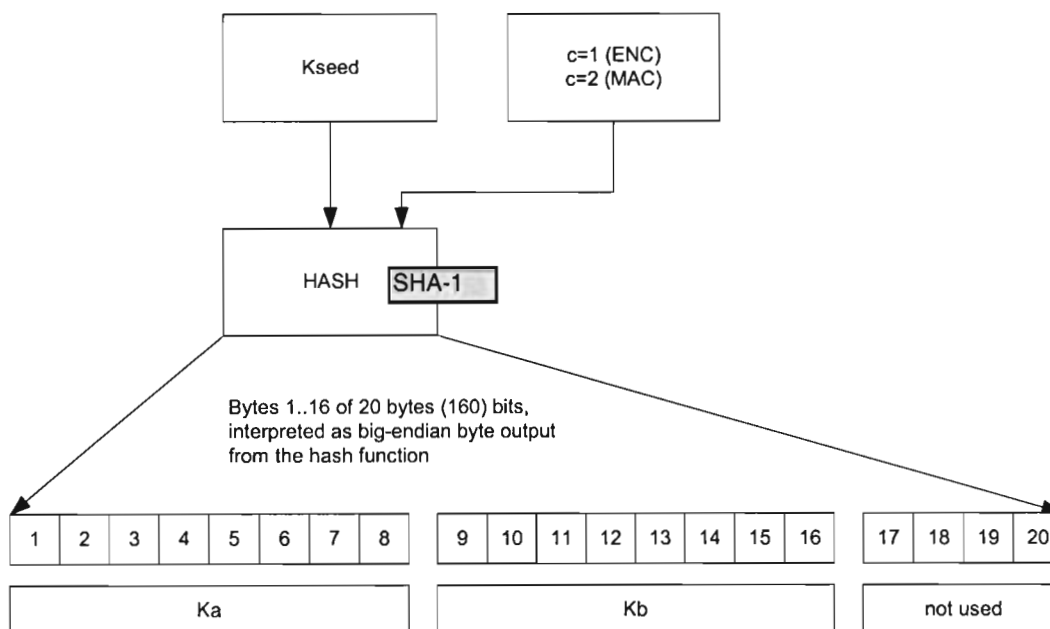


Figure 1: Compute keys from key seed scheme

E.2 Authentication and Key Establishment

Authentication and Key Establishment is provided by a three pass challenge-response protocol according to ISO 11770-2 Key Establishment Mechanism 6 using 3DES as block cipher. A cryptographic checksum according to ISO/IEC 9797-1 MAC Algorithm 3 is calculated over and appended to the ciphertexts. The modes of operation described in Annex E.4 MUST be used. Exchanged nonces MUST be of size 8 bytes, exchanged keying material MUST be of size 16 bytes. Distinguishing identifiers MUST NOT be used.

In more detail, IFD and ICC perform the following steps:

Key generation

Produces based on K_{seed}
(which is derived from the NIST)
a 112 bit key 3DES for
encryption
and a 112 bit key 3DES for
authentication

Observe:

3DES is used.

Known (at the time):

DES is broken.

- by differential or linear cryptanalysis
but only theoretically.
- by brute force:

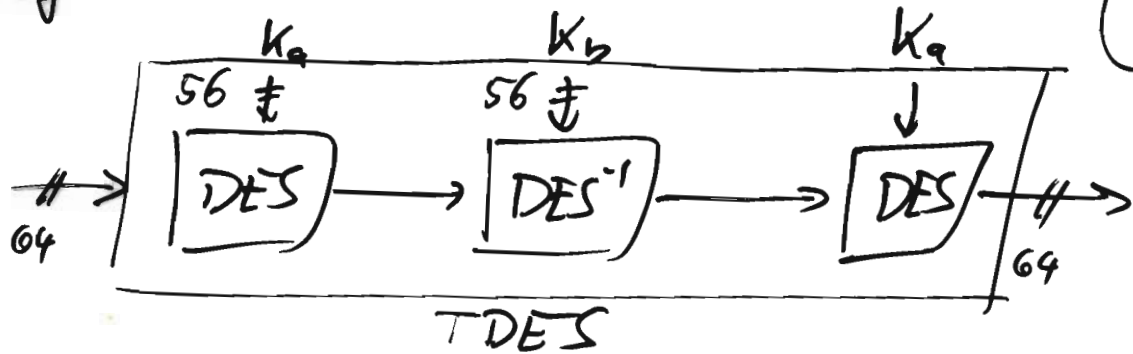
EFF using a \$250'000 special
(?2001?) hardware in runtime 2 days.

Uni Bochum/MPI using \$10'000 standard
(?2004/5?) hardware in runtime 9 days

But: 3DES uses 112 bit key
and is supposed to be secure.
It is slower than 128-bit AES

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⑥

3DES is just triple execution of DES :



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⑦

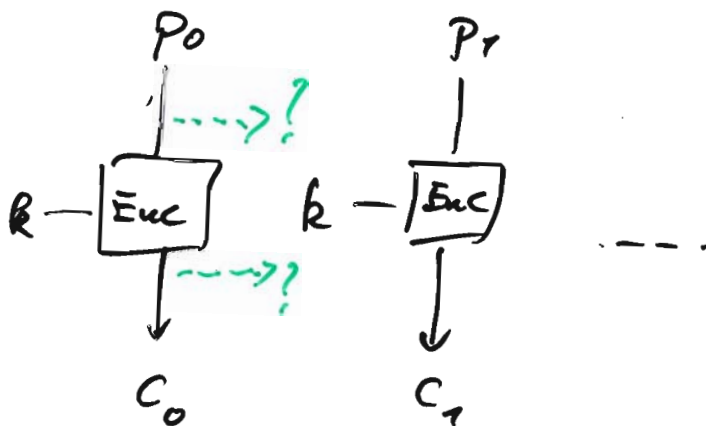
Block cipher into stream cipher
(like TDES, or AES)

16.6.09
⑦

Nodes of operation

Easiest solution :

ECB Electronic codebook



+ Fast self-synchronization

- Simple to modify a single block
- Simple to get plain text - ciphertext pairs
- Same plain text/ciphertext can be used

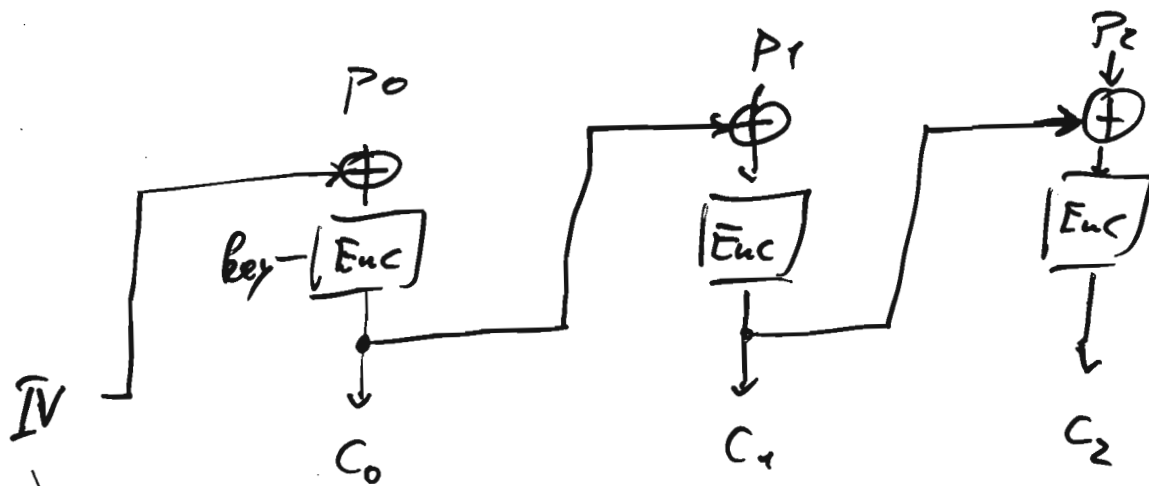
Ways out:

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②

(a) reuse bits from p_0 or c_0
in the encryption of p_1
(and so on...)

(b) use same MAC (message authentication code = kind of a signature) to detect changes

CBC-mode (Cipher Block Chaining)



can be agreed on
or transmitted & chosen at random
or fixed

- + same plaintext yields different ciphertext if we vary the IV
- + fast self-synchronization
- + simple to get plaintext-ciphertext-pairs

Technical Report

PKI for Machine Readable Travel Documents offering ICC read-only access

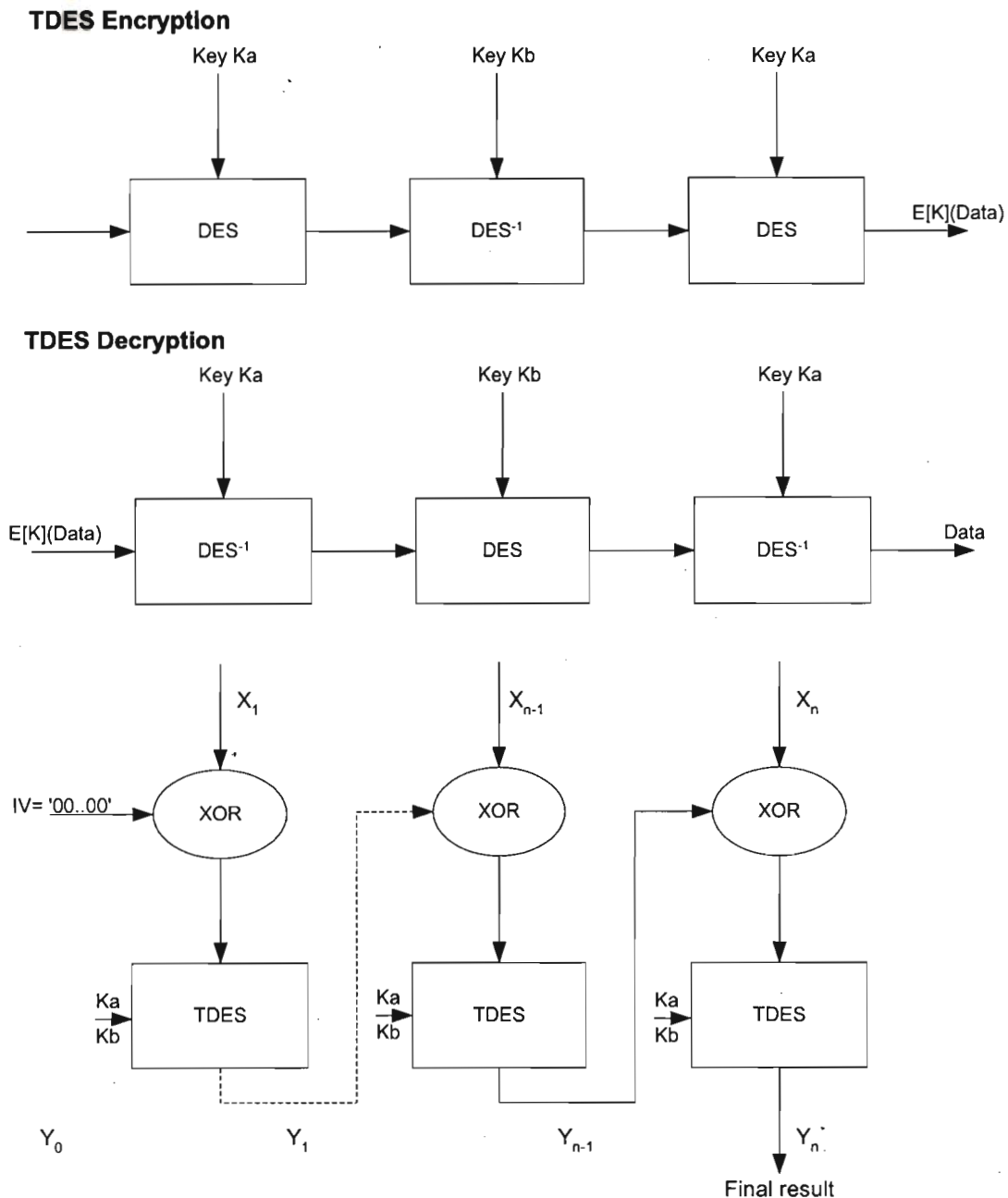
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Date : October 01, 2004

E.4 3DES Modes of Operation

E.4.1 Encryption

Two key 3DES in CBC mode with zero IV (i.e. 0x00 00 00 00 00 00 00 00) according to ISO 11568-2 is used (see diagrams below). No padding for the input data is used when performing the MUTUAL AUTHENTICATE command. During the computation of SM APDUs, padding according to ISO 9797-1 padding method 2 is used.



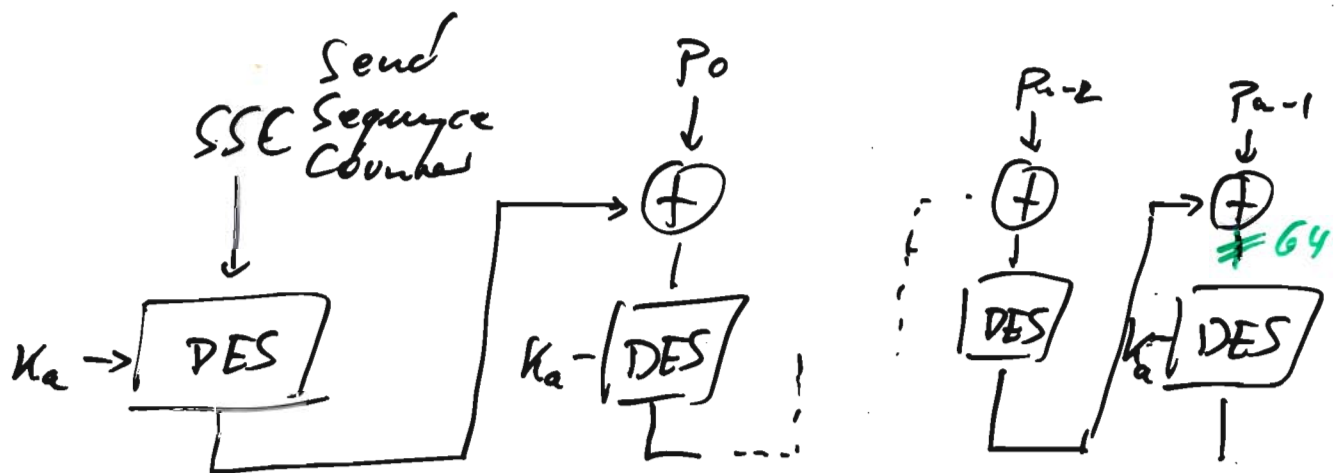
- IV = zero initialization vector
- ' $X_1 || \dots || X_n$ ' = plain text (message to encrypt) where each block X_i is 64-bit long
- ' $Y_1 || \dots || Y_n$ ' = resulting cryptogram (encrypted message) where each block Y_i is 64-bit long

Figure 4: 3DES Encryption/Decryption in CBC Mode

What about integrity?

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③

Specially DES-TDES adapted CBC-like
MAC:



retail MAC

Cryptographic
Checksum

→ compare to other constructions

XCBC-AES ~ HMAC-SHA1

Security: We should prove something like:
if we can forge a cryptographic checksum
then we can break DES or even TDES.

Technical Report

PKI for Machine Readable Travel Documents offering ICC read-only access

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Date : October 01, 2004

E.4.2 Message Authentication

Cryptographic checksums are calculated using ISO/IEC 9797-1 MAC algorithm 3 with block cipher DES, zero IV (8 bytes), and ISO9797-1 padding method 2. The MAC length MUST be 8 bytes.

After a successful authentication the datagram to be MACed MUST be prepended by the Send Sequence Counter. The Send Sequence Counter is computed by concatenating the four least significant bytes of RND.ICC and RND.IFD respectively:

$SSC = RND.ICC \text{ (4 least significant bytes)} \parallel RND.IFD \text{ (4 least significant bytes)}$.

The Send Sequence Counter is increased every time before a MAC is calculated, i.e. if the starting value is x , in the next command the value of SSC is $x+1$. The value of the first response is then $x+2$.

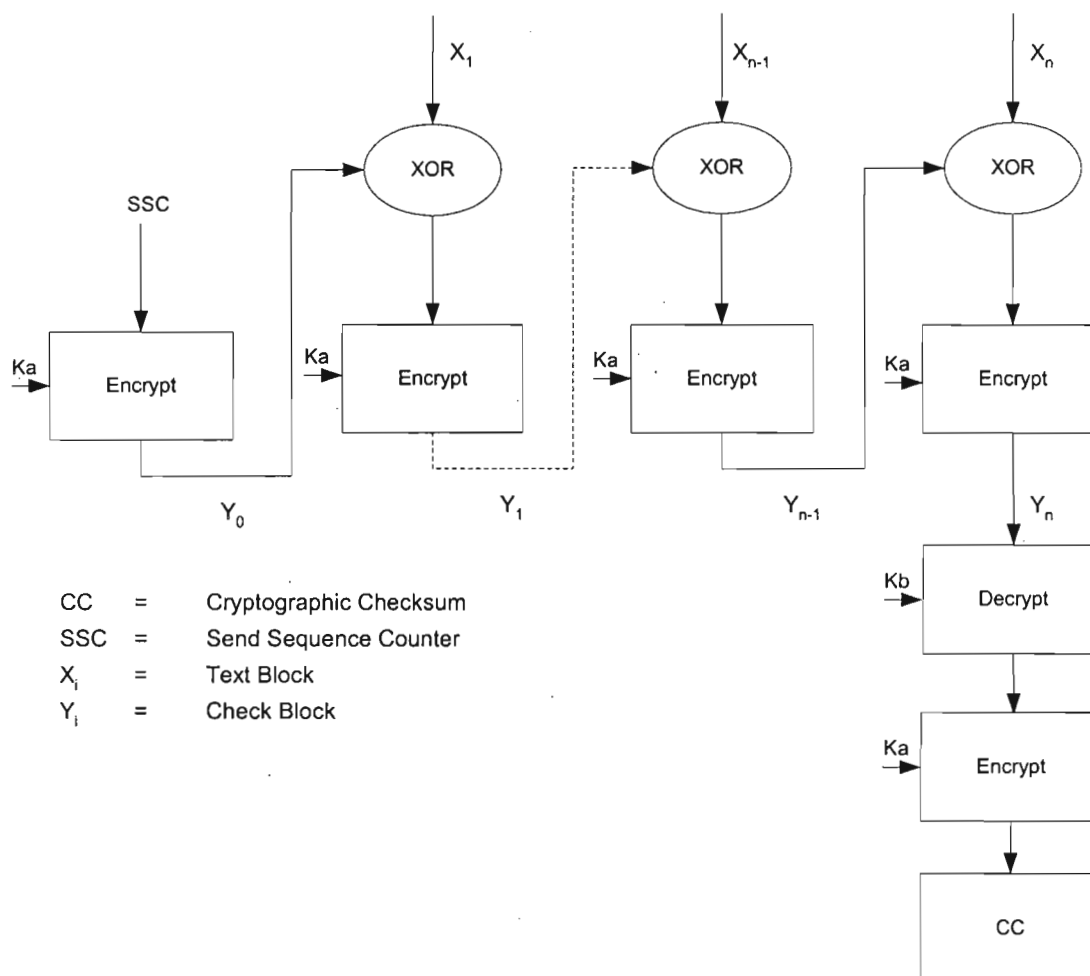
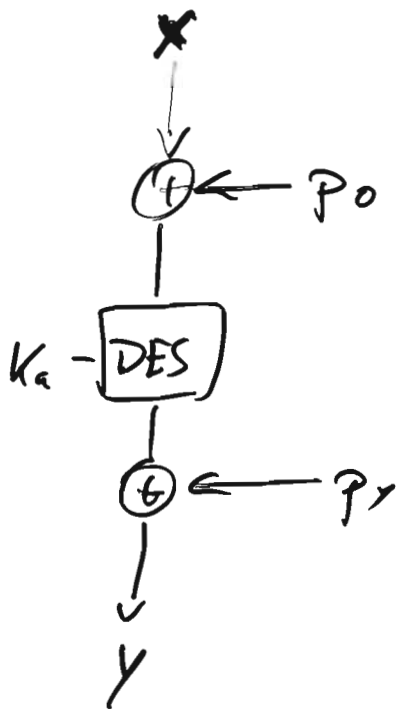


Figure 5: Retail MAC calculation

we should consider the effect of changes to the message.

gb
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(4)



Changing without effect on y ?

$$\text{DES}_{K_a}(p_0 \oplus x) \oplus p_r$$

||

$$\text{DES}_{K_a}(p_0' \oplus x) \oplus p_r'$$

ie. we would have to manipulate p_r' like an encryption.

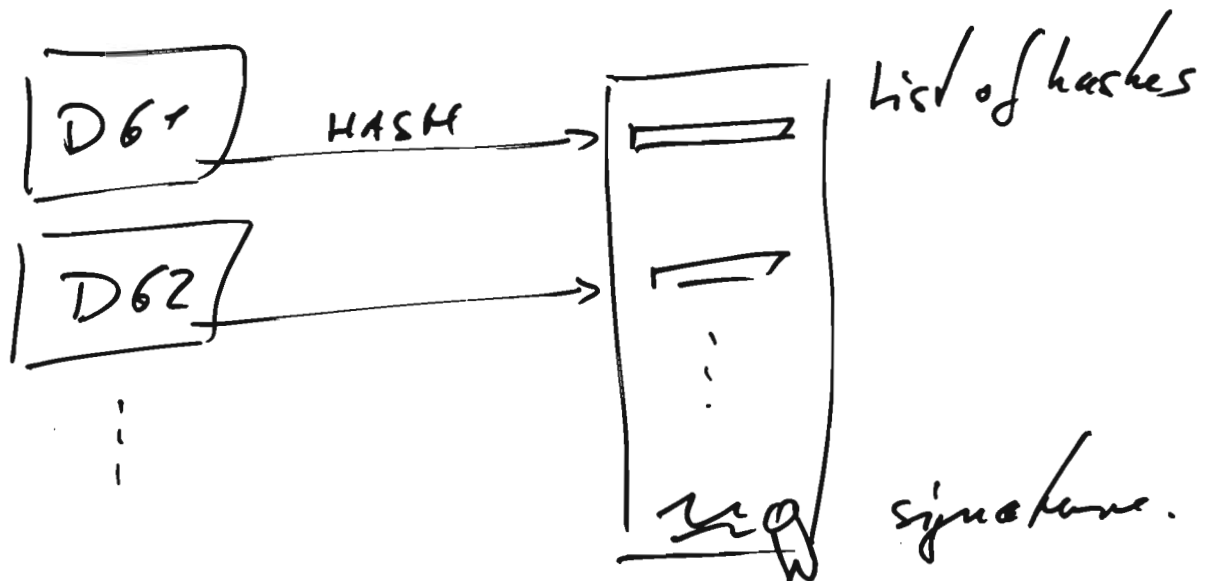
But we cannot encrypt without the key.

So it seems that we need to break at least DES to forge the crypto-checksum.

Logical Data Structure

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17.6.09
④

- Precise definitions down to byte level are given in Doc 9303 about which and how the data are stored.
- All this data has to be 'secured' by a signature.
The construction is as follows:



This grants that the reader can check integrity and authenticity of each single Data Group separately.

CSCA (Germany)

CVCA (Germany)

DS (Germany)

DV (France)

PASS (Germany)

LESEGERÄT (Frz.)

3-5 years

3072
256

0-3 month

2048
224

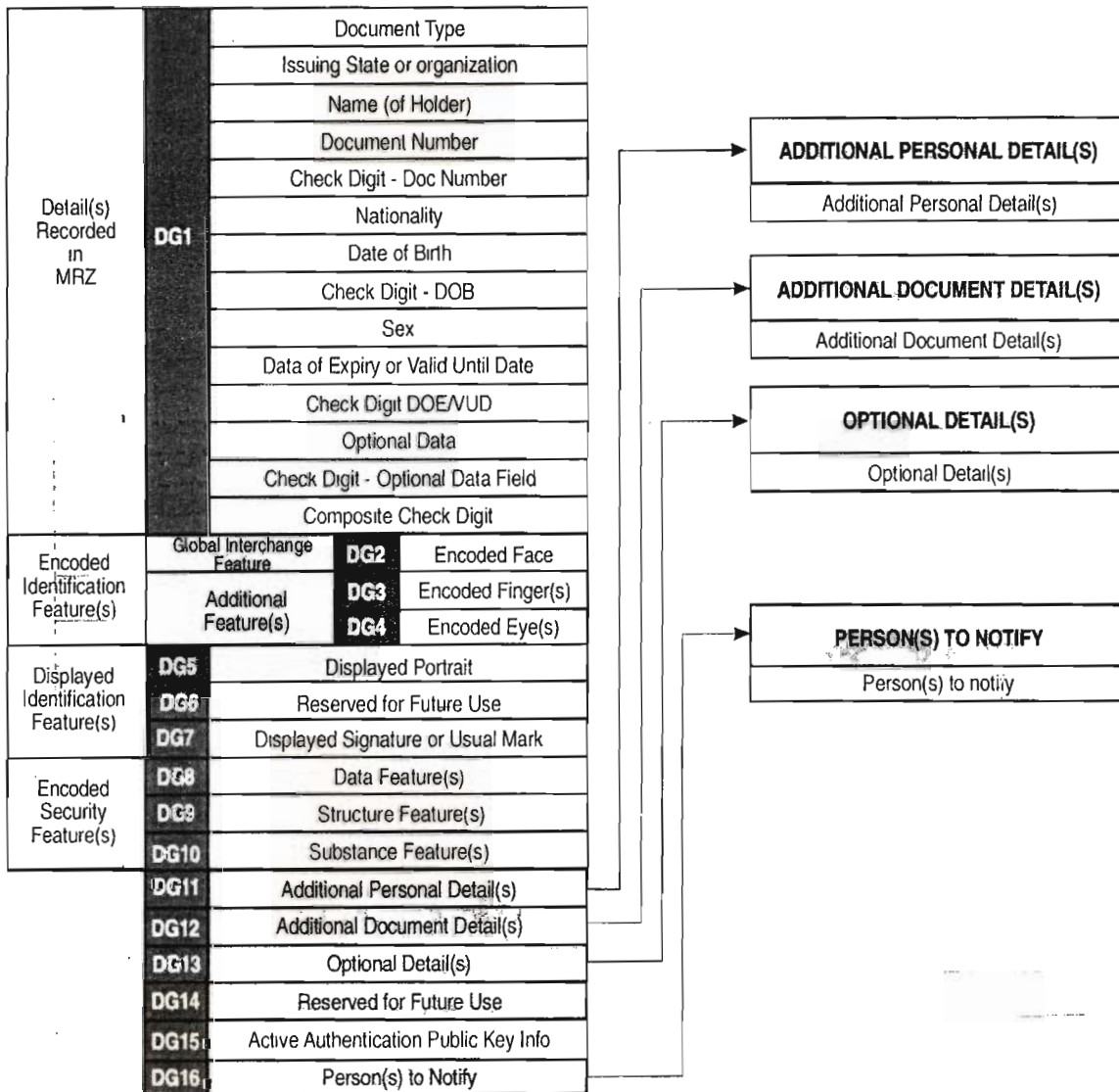
Germany?

France

1024
160

5-10 years

ISSUING STATE or ORGANIZATION RECORDED DATA

FUTURE VERSION OF LDS_{MPTC}

RECEIVING STATE and APPROVED RECEIVING ORGANIZATION RECORDED DATA

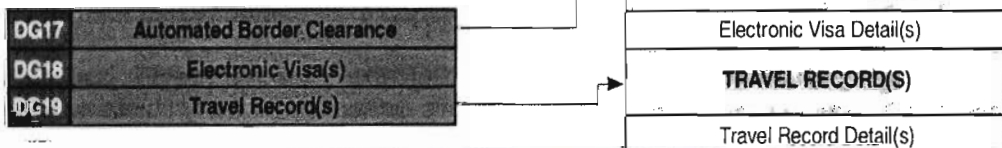


Figure III-2. Data group reference numbers assigned to LDS



Why ICAO Selected the Face as Primary Biometric Identifier specified to ePassports

by ICAO Secretariat

It has long been recognized that names and honour are not sufficient to guarantee that the holder of an identity document (such as a Machine Readable Passport - MRP) assigned to that person by the issuing State is guaranteed to be the person purporting, at a receiving State, to be the same person to whom that document was issued.

The only method of relating a person irrevocably to his travel document is to have a physiological characteristic of that person associated with the travel document in a tamper-proof manner. This physiological characteristic is a biometric.

After a five-year investigation into the operational needs for a biometric identifier which combines suitability for use in the MRP issuance procedure and in the various processes in cross-border travel consistent with the privacy laws of

various States, ICAO has specified that facial recognition shall become the globally interoperable biometric technology. A State may also optionally elect to use fingerprint and/or iris recognition in support of facial recognition.

In reaching this conclusion, ICAO observed that for the majority of States the following advantages applied to facial images:

- Facial photographs do not disclose information that the person does not routinely disclose to the general public.
- The photograph (facial image) is already socially and culturally accepted internationally.
- The facial image is already collected and verified routinely as part of the MRP application form process in order to produce a passport to Doc 9303 standards.
- The public is already aware of the capture of a facial image and its use for identity verification purposes.
- The capture of a facial image is non-intrusive. The end user does not have to touch or interact with any physical device for a substantial timeframe to be enrolled.
- Facial image capture does not require new and costly enrollment procedures to be introduced.





- Capture of a facial image can be deployed relatively immediately, and the opportunity to capture facial images retrospectively is also available.
- Many States have a legacy database of facial images captured as part of the digitized production of passport photographs which can be encoded into facial templates and verified for identity comparison purposes.
- In appropriate circumstances, as decided by the issuing State, a facial image can be captured from an endorsed photograph, not requiring the person to be physically present.
- For watch lists, a photograph of the face is generally the only biometric available for comparison.
- Human verification of the biometric against the photograph/person is relatively simple and a familiar process for border control authorities.

Optional additional biometrics

States can optionally provide additional data input to their (and other States) identity verification processes by including multiple biometrics in travel documents, i.e. a combination of face and/or fingerprint and/or iris. This is especially relevant where States may have existing fingerprint or iris databases in place against which they can verify the biometrics proffered to them; for example, as part of an ID card system.

Storage of an optional fingerprint biometric

There are three classes of fingerprint biometric technology: finger image-based systems, finger minutiae-based systems, and finger pattern-based systems. Whilst standards have been developed within these classes to make most systems interoperable amongst their class, they are not interoperable between classes. Three standards for fingerprint interoperability are therefore emerging: storage of the image data, storage of the minutiae data and storage of the pattern data. Where an issuing State elects to provide fingerprint data in its ePassport, the storage of the fingerprint image is mandatory to permit global interoperability between the classes. The storage of an associated template is optional at the discretion of the issuing State.

Storage of an optional iris biometric

Iris biometrics are complicated by the dearth of proven vendors. A de facto standard for iris biometrics has therefore emerged based on the methodology of the one recognized vendor. Other vendors may in future provide iris technology, but it is likely they will need the image of the iris as their starting point, rather than the template created by the current vendor. Where an issuing State elects to provide iris data in its ePassport, the storage of the iris image is mandatory to permit global interoperability. The storage of an associated template is optional at the discretion of the issuing State.

For more on this issue, please see ICAO Doc 9303 Part 1, Volume 2 sixth edition. ♦

Chip authentication

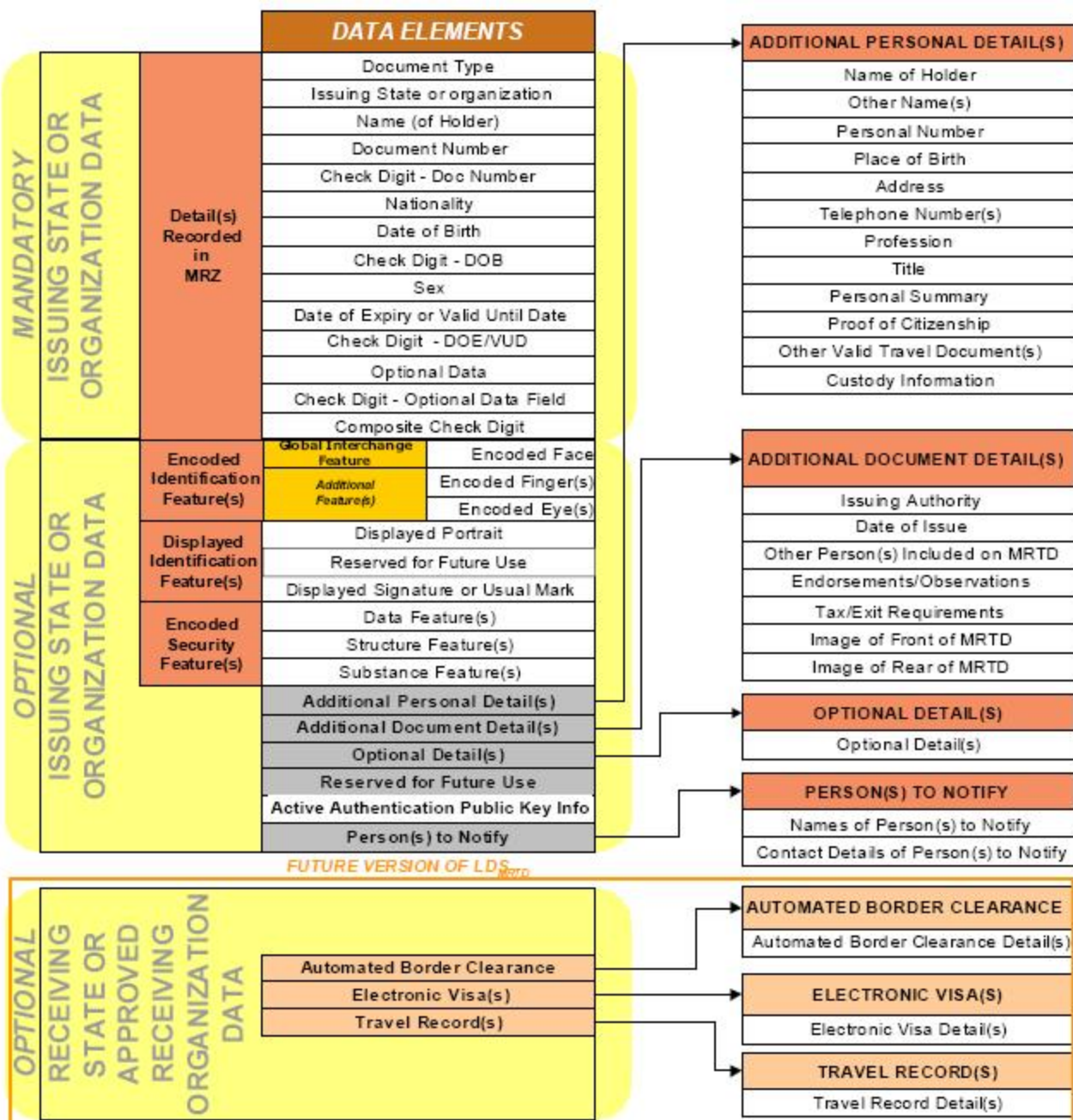
30.6.09
cpl
①

- Chip authentication
(replaces Active Authentication)
- Terminal authentication.
-

Advanced Inspection Procedure

- ① Basic Access Control MUST
↓
(now mandatory)
- ② Chip authentication MUST
(incl. key update (i.e. DH!))
- ↓
- ③ Passive authentication MUST
(read the security object
and check its signature)
- ↙ ↘
- ④ Read less-sensitive data OPT.
- ↓
- ⑤ Terminal authentication OPT.
- ↘
- ⑥ Read sensitive data OPT.
as fast as the reader's
certificate allows

(based on TR by BSI 2004 / 2009)



Inlay with integrated
contactless chip

Passport cover

laminated
protective layer

Data page with
data and photograph

Inlay with
contactless chip

laminated
protective layer

Contactless module

Integrated Circuit

Antenna

► The contactless chip can be integrated into either the cover page or the data page.

Technical Report

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Response APDU	Mandatory if data is returned, otherwise absent.	Not used	Mandatory, only absent if SM error occurs.	Mandatory if DO'87' and/or DO'99' is present.
---------------	--	----------	--	---

Table 1: Usage of SM Data Objects

Figure 2 shows the transformation of an unprotected command APDU to a protected command APDU in the case *Data* and *Le* are available. If no *Data* is available, leave building DO '87' out. If *Le* is not available, leave building DO '97' out.

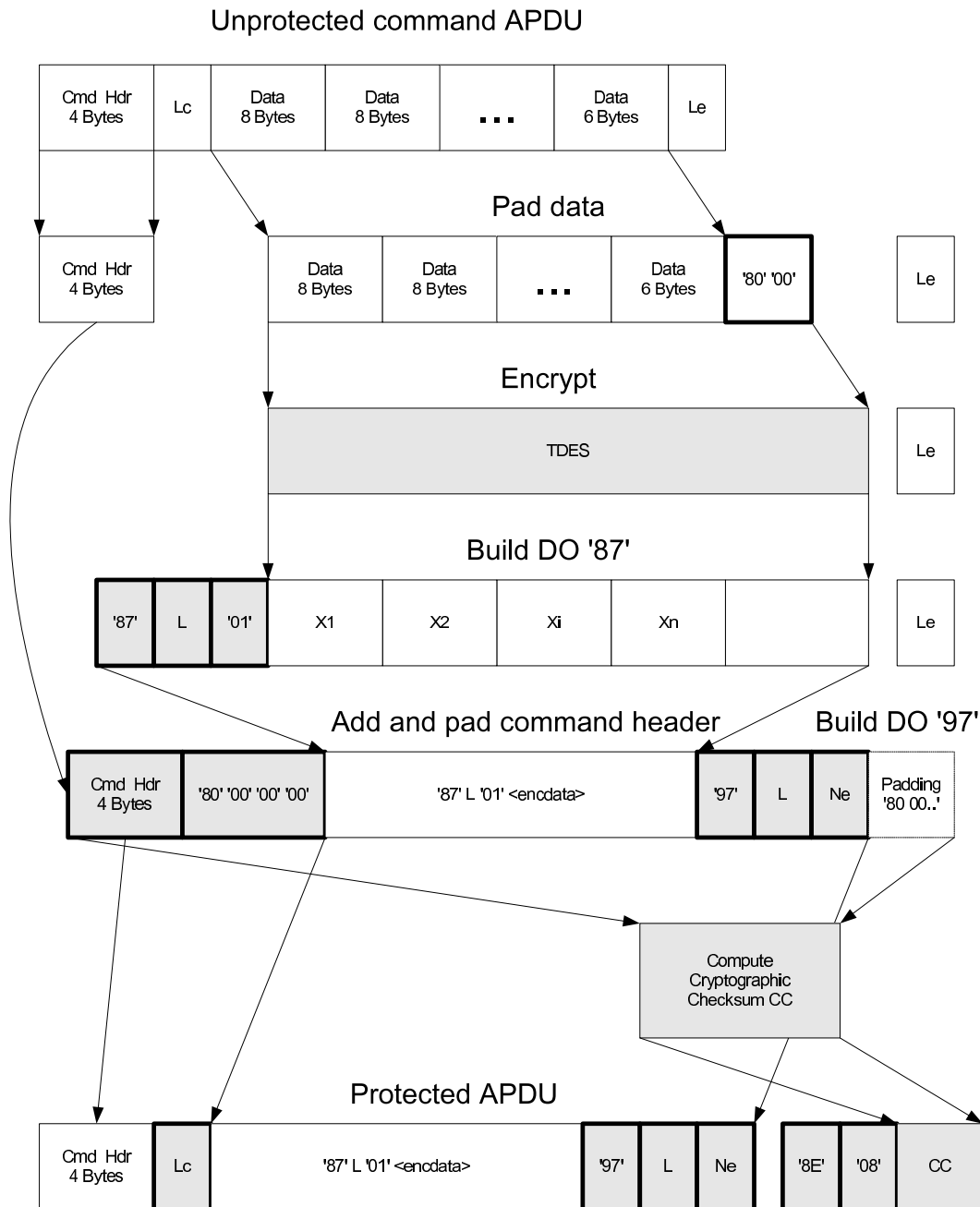


Figure 2: Computation of a SM command APDU

The protocols

cpb
30.6.09
(2)

Chip authentication

Passport

static key pair

$(SK_{icc}, PK_{icc}, D_{icc})$

Reader

$(\gamma, g^\gamma, g \in G)$

$(s, g^s, g \in G)$
signed via SO_D

PK_{icc}, D_{icc}

choose random
ephemeral
key pair

$(\tilde{SK}_{FD}, \tilde{PK}_{FD}, D_{icc})$

$g^{\gamma s}$
 $= (g^\gamma)^s$

\tilde{PK}_{FD}

$KA(SK_{icc}, \tilde{PK}_{FD}, D_{icc}) = KA(\tilde{SK}_{FD}, PK_{icc}, D_{icc})$

serves as
new K_{seed} .

This replaces active authentication and increases the security of the following conversation since the Diffie Hellman key exchange has "perfect forward security".

Repetition:

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①

HORTON's principle

We must always authenticate
the meaning of the message.

(i.e. auth. the plaintext is fine,
but auth. the ciphertext is not sufficient.)

We can use either

AE Authenticate then Encrypt.

or

EA Encrypt & authenticate.

In the second case we have to be aware
that the authentication mechanism
gets the ciphertext, so we seem to violate
HORTON's principle.

We can authenticate ciphertext + enc.-key
determines the plaintext
or authenticate using ~~a key~~ an auth.-key
which is strongly related to the
encryption key.

↗
This happens in the MRTD protocols.

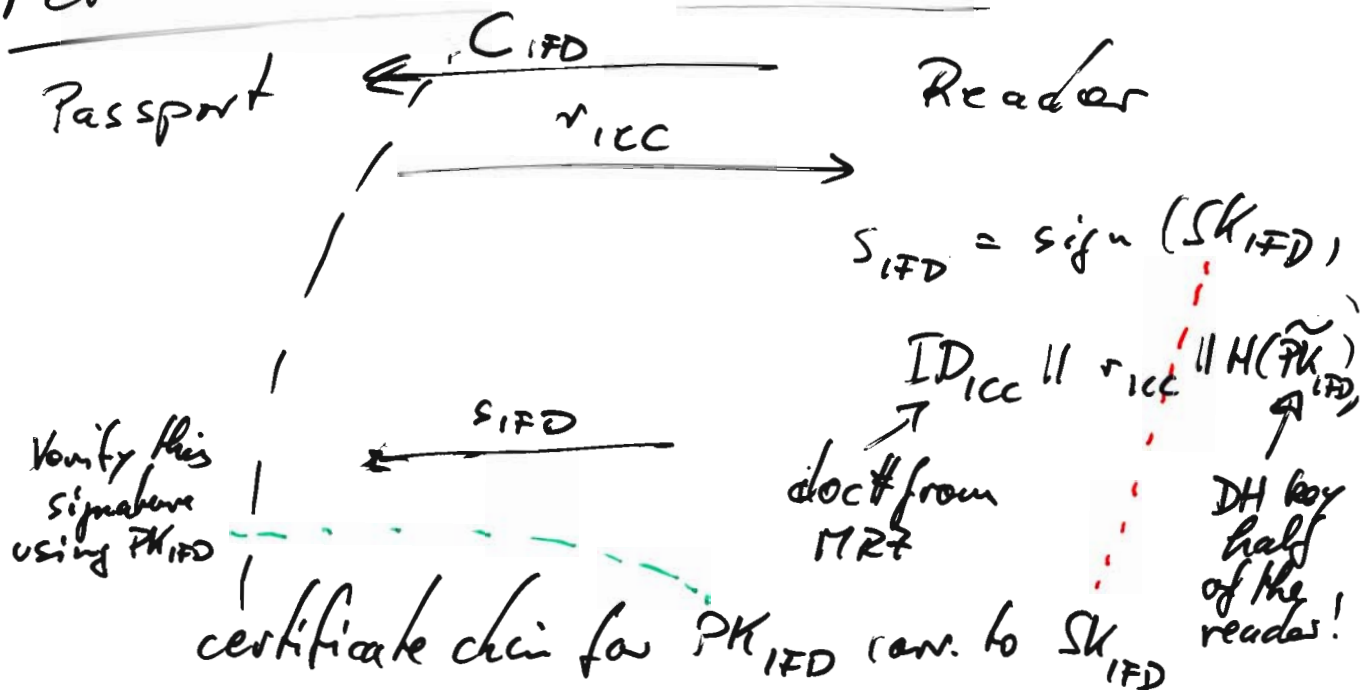
After setting up a secured connection via a certain key agreement protocol (for example Diffie-Hellman) we can bind authentication results to the agreed key. Thus you do need to reauthenticate every message!

sp6
1.7.09
(2)

The "authentication" in the chip authentication protocol is provided by subsequent verification of the SO_D , the passive authentication.

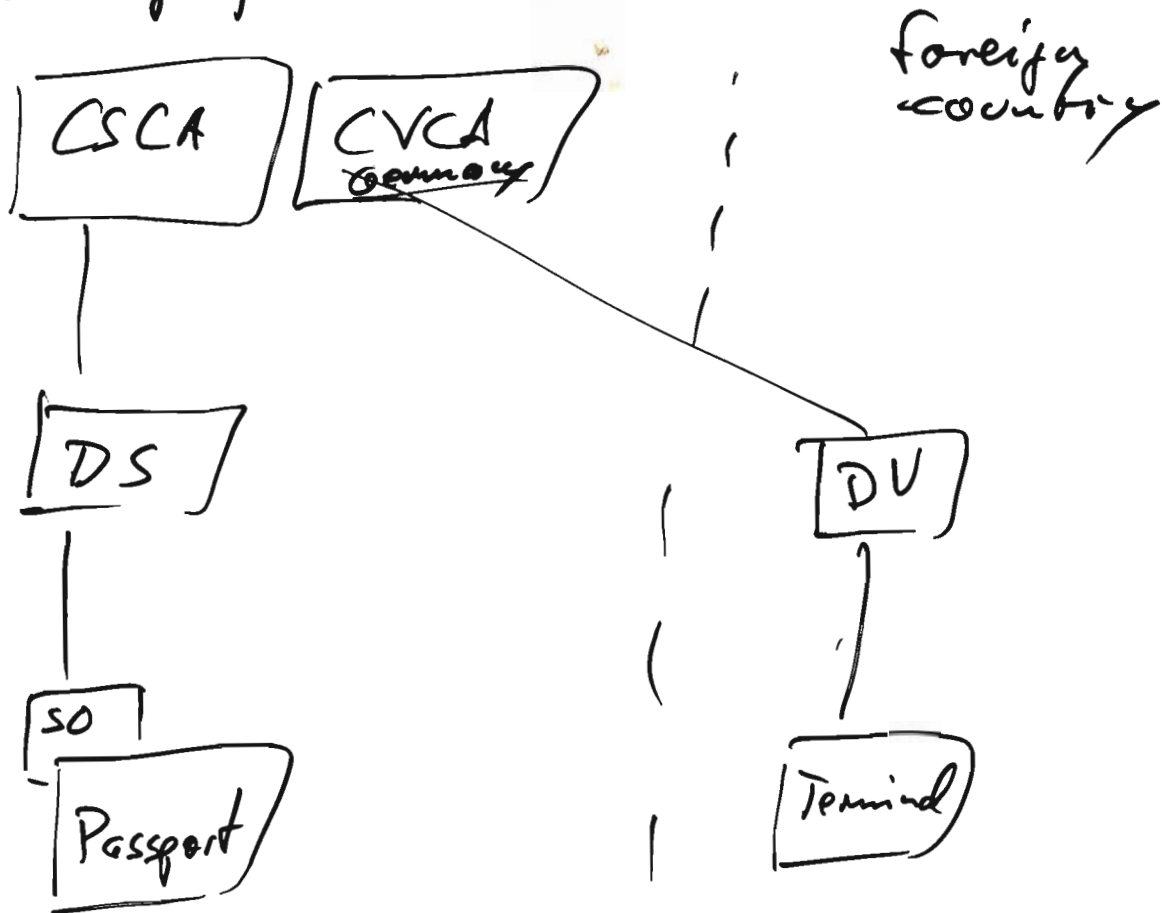
Last open point:

Terminal authentication



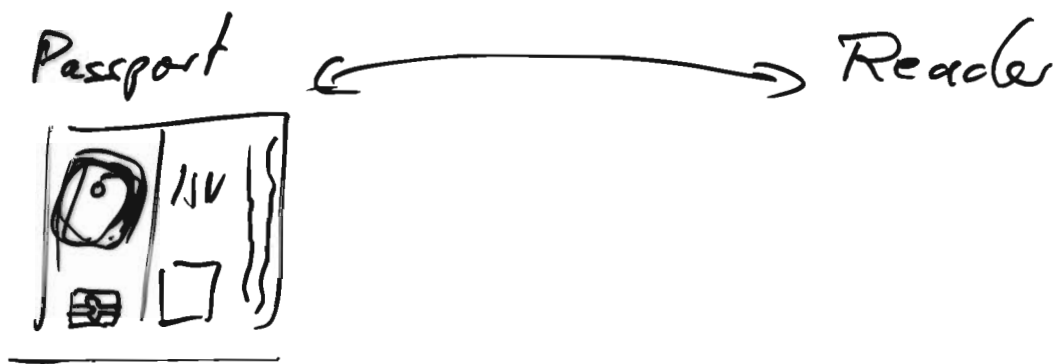
We have make sure that the chip knows the root certificate C_{CVCA} of the country verification ~~E~~certification authority. So we store it on the chip during production.

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(3)



Mind sovereignty of each country!

(Eg. the CSCA and CVCA certificates are not distributed publicly but only by diplomatic means.)



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④

(a) Nicely structured data

(b) various auth. & means:

BAC \rightarrow grants the nobody can talk or listen without the MR7

Passive auth. \rightarrow chip info cannot be changed.

EAC : chip auth. (& DH!)

\rightarrow chip not cloned
 \rightarrow perfect forward security

terminal auth

\rightarrow chip can check privileges of the reader.

Need two PKI, one for signing and another for verification.

Ask questions!

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1.7.09
⑤

What prevents chip cloning?

Why is step ② before step ③
in the Advanced Inspection
Procedure?

What grants confidentiality
of the conversation between
chip and reader?

Can an attacker - with or
without knowledge of MRZ -
identify a certain passport,
say to trigger a bomb?

Biometrics

CP6
7.7.05
(7)

focused on fingerprint

Intentions?

- Verify or recognize the identity of a living human individual.
- automated methods.

based on physiological or behavioral characteristics.

Examples of biometrics:

- finger prints
- iris scans
- voice
- face 2D, 3D
- gait
- handwriting
- hand geometry
- ear
- teeth
- (smell)
- DNA)
- patterns
- genome

History related fingerprints

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(2)

≈ 6000 BC fingerprints on pottery,
on houses,
on business records.

1686 Marcello Malpighi
→ ridges, spirals, loops

1823 John Portinji (Breslau)
→ nine fingerprint patterns

1880 Alphonse Bertillon (Paris)
→ system of anthropometry
to classify criminals
and to identify recidivists
↳ height, weight, length of arm, leg,
index finger

I ≈ 1904 case "William West"

1856 Sir William Herschel (Jungipoor, India)
→ used palmprints (and fingerprints)
to certify contracts
with native people
PLAYING on their superstition.

→ observed, as his collection grew, that fingerprints can prove or disprove identity.

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(3)

1870 Dr Henry Faulds (British surgeon, Japan)
- noticed finger marks on ancient pottery
→ classification method.
→ first to identify greasy fingerprint on an alcohol bottle.

1880s Francis Galton

1892 book "Fingerprints"

→ fingerprints are permanent throughout life

→ no two are identical

(prob $\sim 1: 64 \cdot 10^3$)

• Galton pattern types

• minutiae, Galton details



1891 Juan Vucetich (Argentina, police officer)
→ first systematic filing of fingerprints using Galton pattern types

1892 ... identified a murderer using a bloody fingerprint

1897 Sir Edward Henry (British police officer, India) CP1
7.7.09
(4)

→ modified fingerprint classification based Galton's observations so that you can easily scan for various criteria ...
→ Henry classification

1901 → adopted by Scotland Yard.

1902 first in USA: NY Civil Services Comm.

1903 NY state prison system

} US military, many state &

1920 local law enforcement agencies

1924 FBI establishes Identification Division by an act of Congress (based on Henry)

1971 > 200 mio fingerprints
MANUALLY

Manual card files

475
7.7.09
5

Henry system

numerical weights to finger
with a whorl pattern

→ bin number $\in \{0, \dots, 1023\}$

Letter symbols assigned to
fingers

→ subdivide bins

Problems . assigned pattern may vary
on the same card

. pattern type error

→ wrong bin

→ no result

later, in early automation

FRIR $\approx 25\%$ estimated.

False reject rate

. further complication:

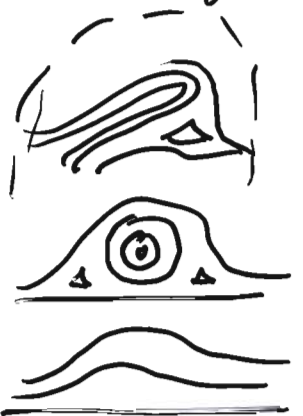
- distribution of pattern types
is not uniform

loop 65%

whorl 30%

arch 5%

solution: subdivide large bins ...



Still: Henry (8 Vucetich) system
allowed to search large files
though the FRR might have
been high.

q6
7.7.09
⑥

and eq. : arches not further
subdivided.

Searching time was long

mid 1960s:

FBI Identification Division
processed ~25000 requests/day
in a criminal file of >20 mio tenprints
using several thousand employees.
→ high FRR

US NBS/NIST supported by FBI

- automated digitization
of inked fingerprints
(invent scanners!)
- effect of image compression
- classification
- extract minutiae
- watching

Technology

late 1960s

(*) { 1.5 in x 1.5 in
500 dpi
effective spotsize 0.0015 in (≈ 1000 dpi)
signal to noise ratio $> 100:1$
 ≥ 64 gray levels, 6-bit

qb
8.7.09
(7)

early 1970s : 5 machines built,

250 fingerprints / h.

used til 1978

→ to digitize 22 mio fingerprints

early 1980s: "low cost" scanners

~ 1990

IAFIS

Integrated Automated Fingerprint
Identification System

App-F : public specification of (*)
+ ≥ 200 effective gray levels

today: . 1.5 x 1.5 in @ ≥ 1000 dpi

. 10-12 bits gray level

. S/N $> 100:1$

...

& directly from fingers "live scan"

Automated fingerprint identification

14.7.09
cpb
⑦

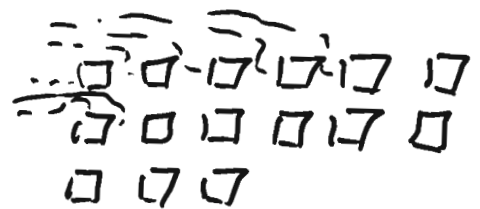
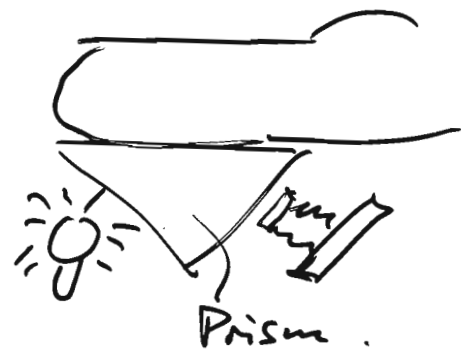
eg. IAFIS (FBI)

Principal method

1. Fingerprint classification
2. Minutiae
3. • Poor positions along ridges
• Patterns formed by the ridge edges

Sensors

- optical sensors
- capacitive silicon
- electric field sensors
- thermoelectric sweep sensor
(IPAQ 65400 Pocket PC)
- ultrasonic sensor
- pressure array



Questions / criteria?

14.7.09
cpb
②

- cost
- robustness, resistance to aging
- power consumption
- size
- dot pitch
- behaviour under electro-static discharge -
- environmental operation for sweaty and dry fingers
- usability, ...
- resistance against misuse (liveliness?)

Testing & identification — Algorithm?

→ FVC2002 (Fingerprint Verification Competition)

4 databases } one synthetic
others from different sensors.

sample size ≈ 90 , average age ≈ 20

Sensor	Equal error rate	FNMR at FMR 1%	FNMR at FMR 0.1%
Optical	0.1%	0.11%	0.21%
Capacitive	0.37%	0.32%	0.61%

Research projects (of ≈ 2003)

14.7.03
③
qb

- Device interoperability
- Lightweight fingerprint verification
- Fingerprint watermarking (?)
- Secure devices
- Continuous classification systems
 - translate fingerprint to a vector so that 'close' means similar
- Pattern matching algorithms.
- Fingerprint image mosaicing techniques
- Fingerprint video recognition

Outlook

- PDAs
- Laptop PCs !
- mobile phones
- secure mass storage
- cars

Local Extracting information from fingerprint images

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15.7.09
①

1. Improve image

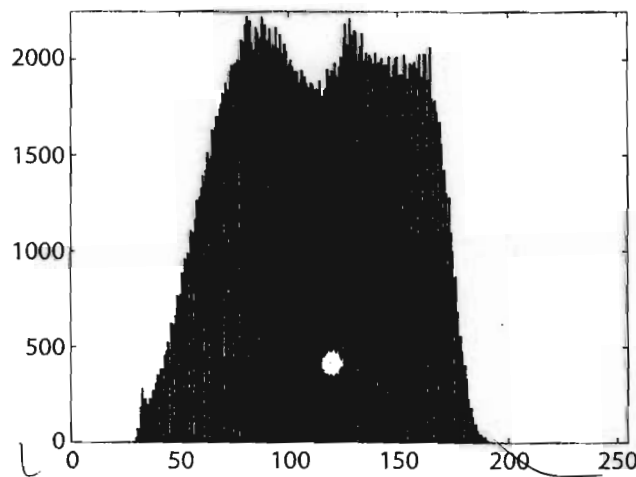


(a)

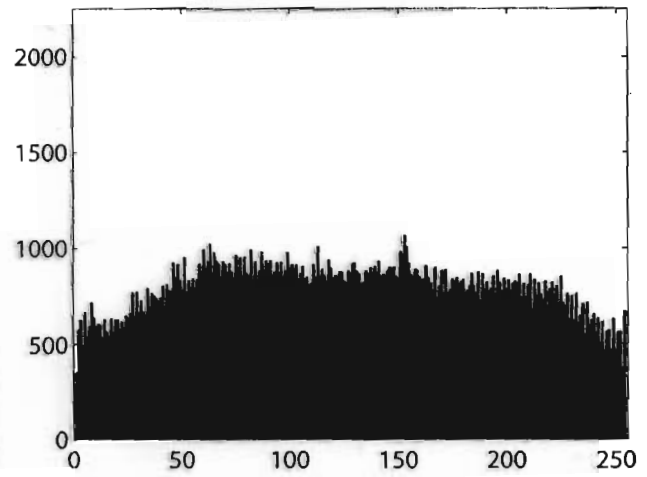


(b)

Figure 2.3 (a) An inked fingerprint image; (b) the results of the local area contrast enhancement algorithm on (a).



(a)



(b)

local area contrast enhancement (LACE)

$$\text{pixel gain} = c \cdot \text{global mean} \cdot \frac{1}{\text{local area std dev}}$$

↑
global correction, empirically determined, eg. $c = \frac{1}{2}$.

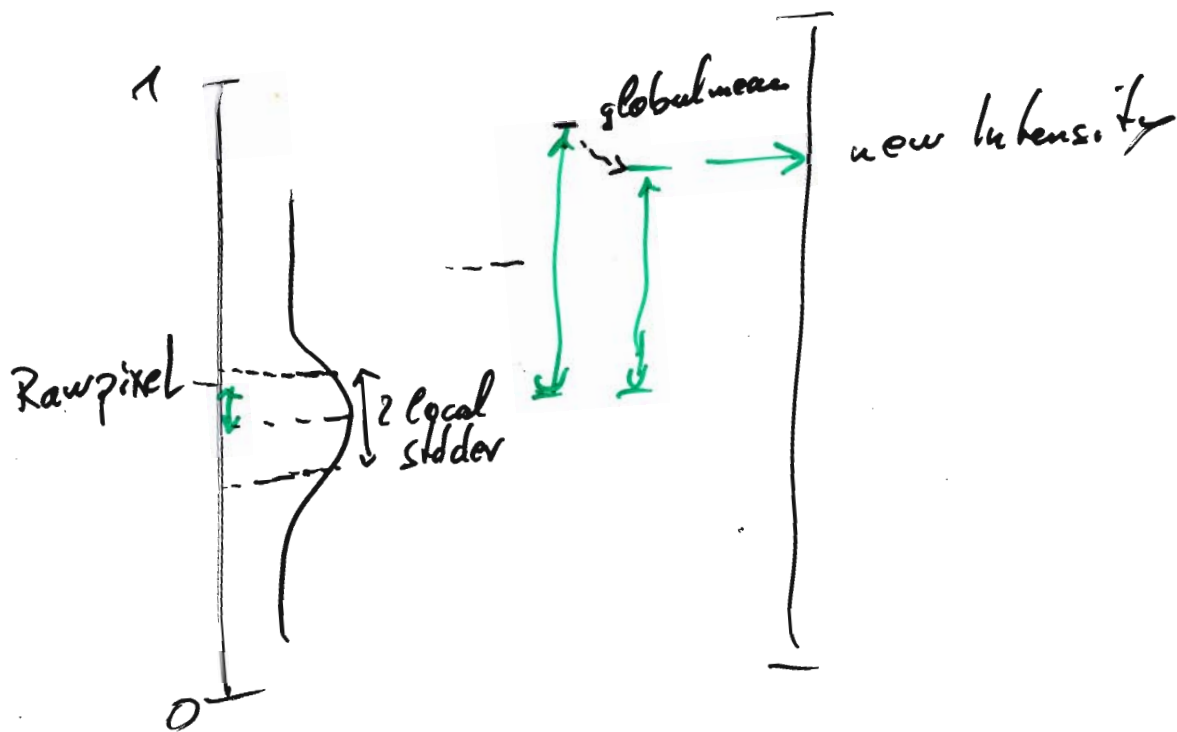


local area is a, say, 15×15 pixel window centered at the considered point

New Intensity

$$= \text{Pixel gain}(\text{Raw Pixel} - \text{local mean}) + \text{local mean}$$

db
15.7.09
(2)

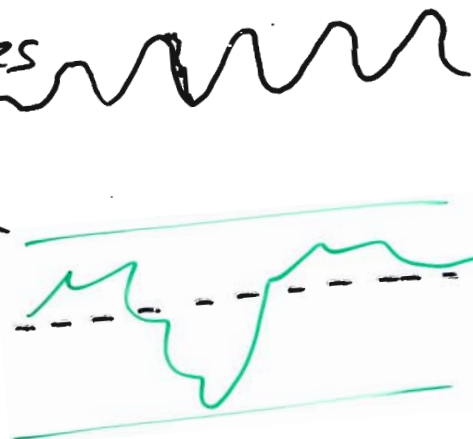
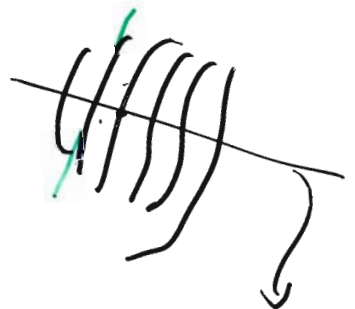


2. Contextual filtering

Amplify expected structure

todo : ① provide band pass filter
orthogonal to the ridges
[high pass]

② provide low pass filter
along the ridges



discovers : Gabor filter.

$$g\left(\underbrace{x, y}_{\text{distance to considered point}}; \underbrace{\sigma_x, \sigma_y}_{\text{damping in x and y direction}}, \underbrace{f}_{\text{frequency "of ridges"}}$$

$$= \exp\left(-\frac{1}{2}\left(\frac{x^2}{\sigma_x^2} + \frac{y^2}{\sigma_y^2}\right)\right) \cdot \cos(2\pi f \cdot x)$$

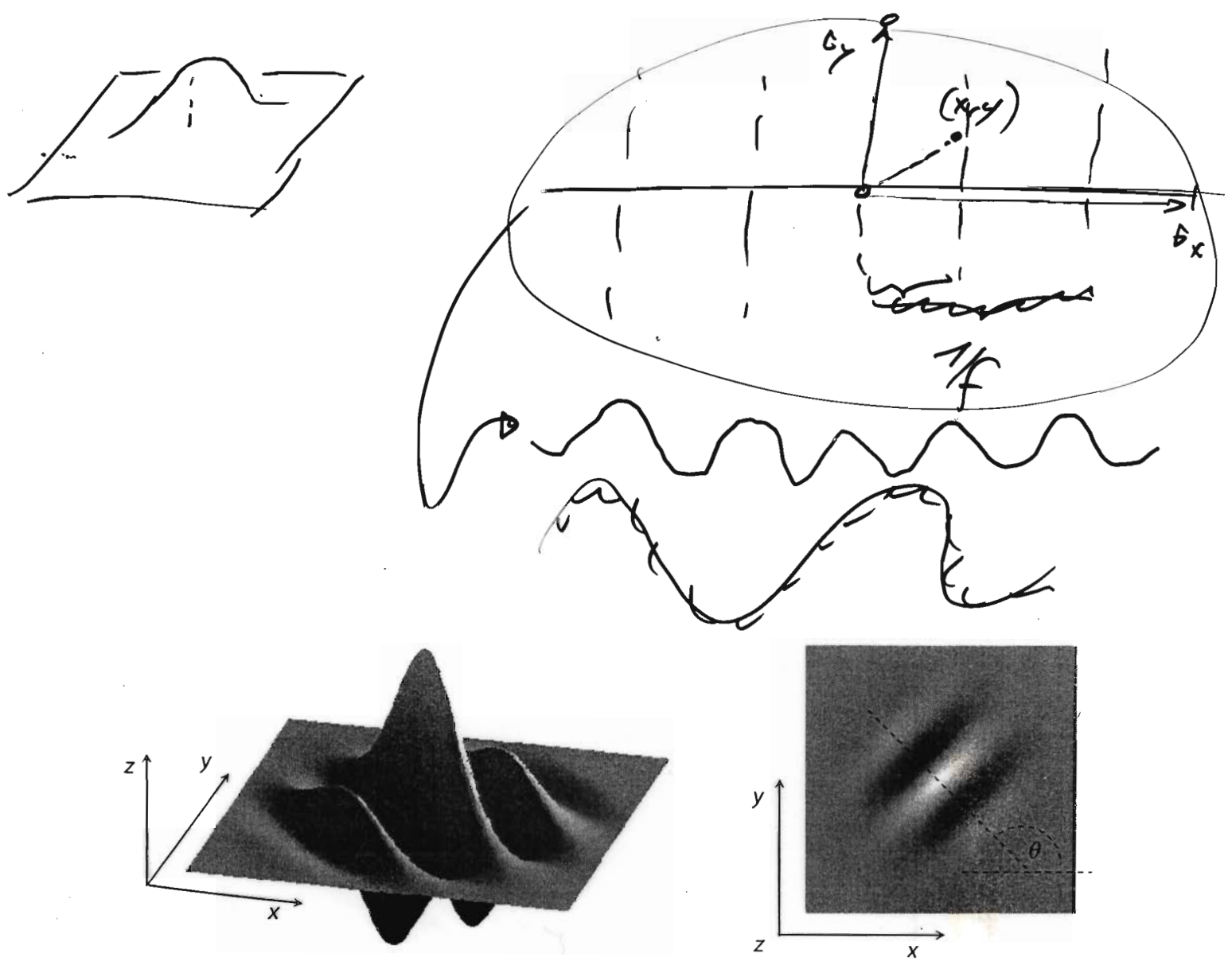


Figure 2.5 Graphical representation (lateral view and top view) of the Gabor filter defined by the parameters $\theta = 135^\circ, f = 1/5, \sigma_x = \sigma_y = 3$ [21].

$$\text{New Pixel} = \sum_{a,b} \underbrace{g(a,b)}_{\text{Filter function (may be rotated!)}} \cdot \text{Pixel}(x+a, y+b)$$

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(4)

This does what we want:

- if the ridge frequency coincides with the filter frequency then the ridges are emphasized.
(Otherwise they are damped.)
- if the ridge direction is parallel to the filter direction then it will be emphasized.
- Being in a valley or on a ridge will be amplified.



(a)



(b)

Figure 2.7 The orientation field is superimposed on the fingerprint image in (a). In (b) of the Gabor filters-based contextual filtering of the fingerprint image in Figure 2.3(a)

This nicely smoothes out the picture! pb
15.7.05
(5)
Cool!

However, we need ridge frequency
and ridge direction
for every pixel!

What we have is a function

$(x, y) \mapsto$ gray level of
pixel x, y

on some integer raster.

First idea: use derivatives

$\begin{bmatrix} \frac{\partial I}{\partial x} \\ \frac{\partial I}{\partial y} \end{bmatrix}$ = gradient of the intensity
↑
"shortest way to the maximum"

Refinements: angle $\approx \arctan \left(\frac{\frac{\partial I}{\partial y}}{\frac{\partial I}{\partial x}} \right)$

Problem: not stable enough.

One uses:

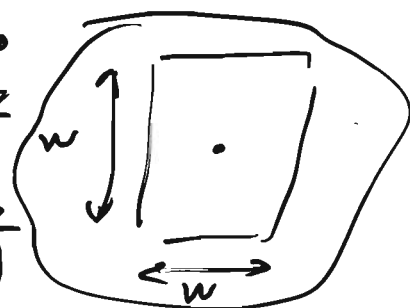
$$\theta(x, y) = 90^\circ + \frac{1}{2} \arctan\left(\frac{2 G_{xy}}{G_{xx} - G_{yy}}\right)$$

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15.7.03
⑥

$$G_{xy} = \sum_{-\frac{w}{2} \leq h, k \leq \frac{w}{2}} \frac{\partial I}{\partial x}(x+h, y+k) \frac{\partial I}{\partial y}(x+h, y+k)$$

$$G_{xx} = \sum_{h, k} \left(\frac{\partial I}{\partial x}(x+h, y+k) \right)^2$$

$$G_{yy} = \sum_{h, k} \left(\frac{\partial I}{\partial y}(x+h, y+k) \right)^2$$



eg. $w = 15$.

and compute the derivatives
via a Sobel filter

-1	1
-2	2
-1	1

This gives us the directions.
Still need the local ridge frequency f .

We still miss the ridge frequency! cpb
22.7.9
①
Take a cross cut orthogonal
to the determined ridge direction

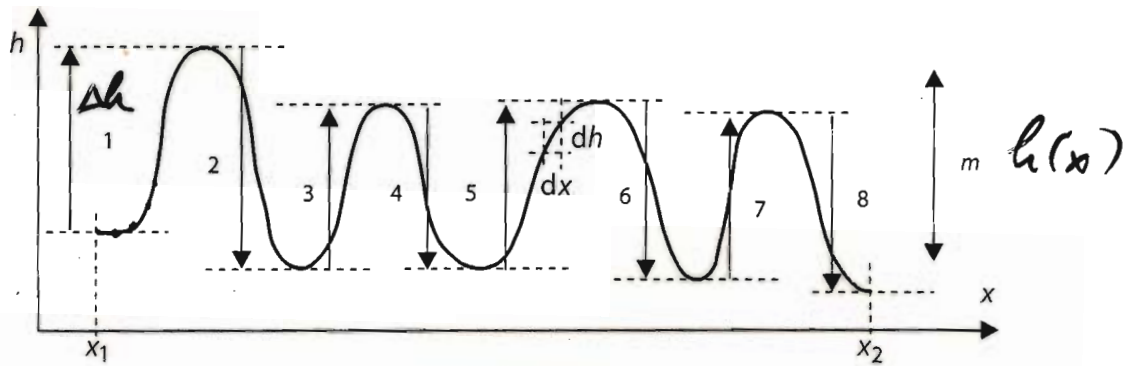


Figure 2.6 The variation of the function h in the interval $[x_1, x_2]$ is the sum of amplitudes $\alpha_1, \alpha_2, \dots, \alpha_8$ [24]. If the function is periodic or the function amplitude does not change significantly within the interval of interest, the average amplitude α_m can be used to approximate the individual α . Then the variation may be expressed as $2\alpha_m$ multiplied by the number of periods of the function over the interval [21].

We consider the total variation:

$$V(h) = \int_{x_0 - k}^{x_0 + k} |h'(x)| dx \quad (\text{local view})$$

$$\text{average amplitude} = \frac{\sum |(\Delta h)(x_i)|}{\# i} \quad (\text{global view})$$

$$V(h) = 2k \cdot 2 \text{ average amplitude} \cdot f$$

$$\Rightarrow f = \frac{\int_{x_0 - k}^{x_0 + k} |h'(x)| dx}{2k \cdot 2 \text{ average amplitude}}$$

In practice average over a small interval

Now we are ready to forget details. cpb
24.7.9
(2)

The next step is :

- choose a threshold and make the picture b/w (two colors!)
- thin out ridges til they are only one pixel wide.

Finally: determine classification and fine structure.

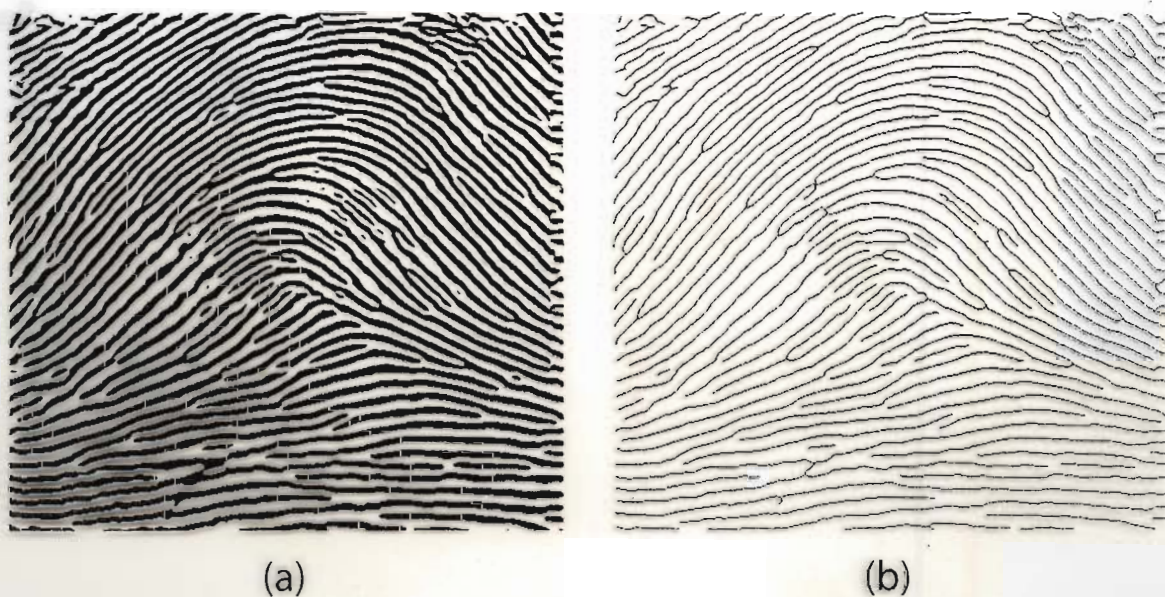


Figure 2.8 (a) shows the result of binarization (through the ridge location algorithm of [enhanced fingerprint image in Figure 2.7(b)]. (b) shows the results of thinning the image to single pixel width.

Repair and determine minutiae

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27.7.03
(3)

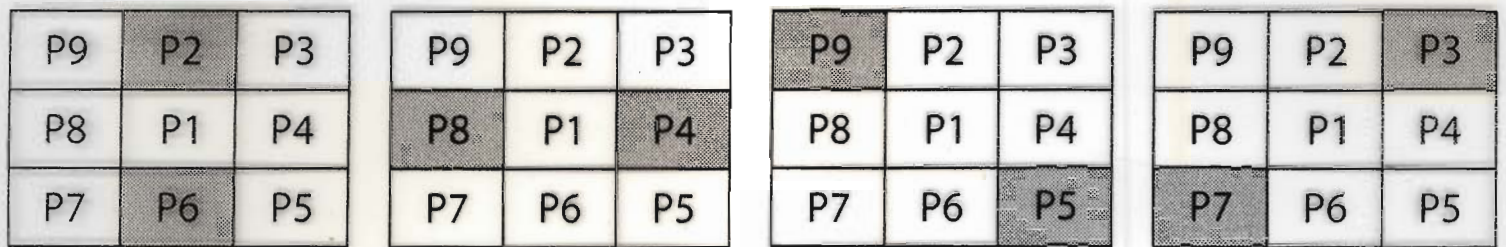
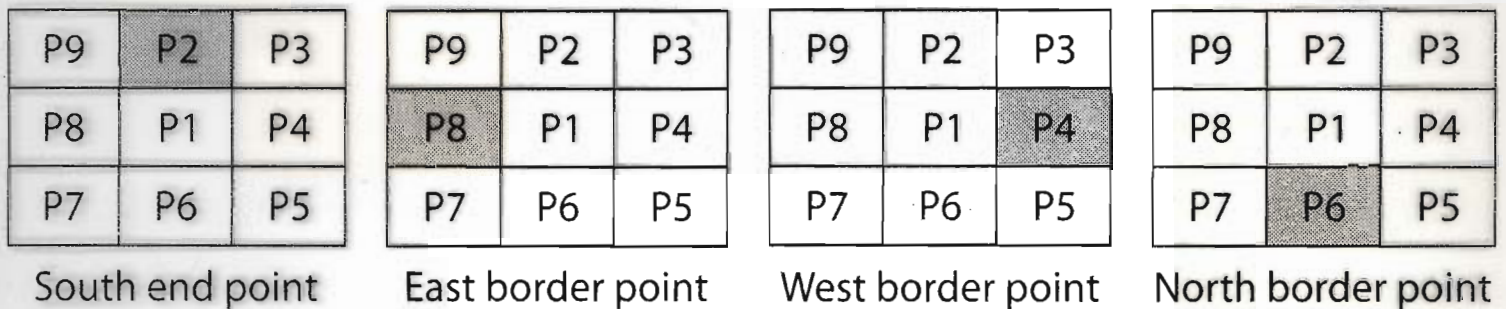


Figure 2.9 Center pixel (P1) is determined to be on a ridge during thinning.

→ Repair and recolor middle pixels in black



South end point

East border point

West border point

North border point

Figure 2.10 Center pixel (P1) is determined to be at the end of a ridge during thinning.

→ Detect line ends!

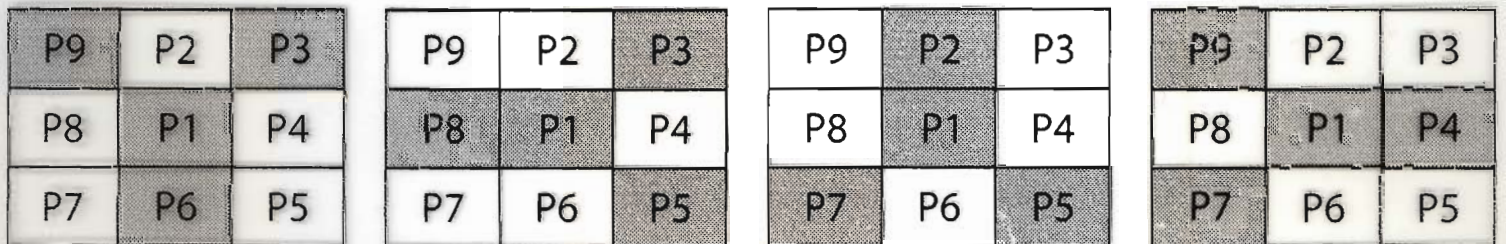


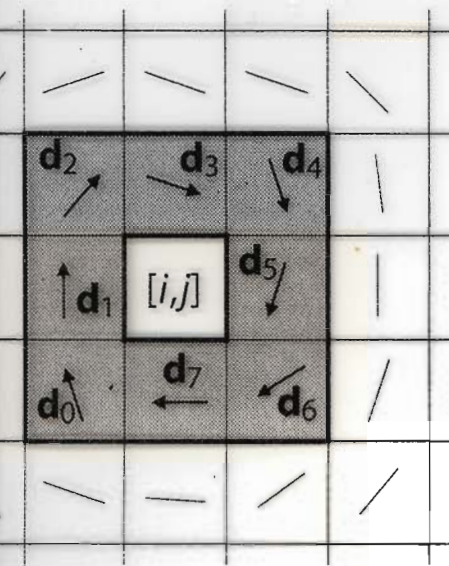
Figure 2.11 Center pixel (P1) is determined to be a ridge bifurcation minutia during thinning.

→ Detect bifurcations!

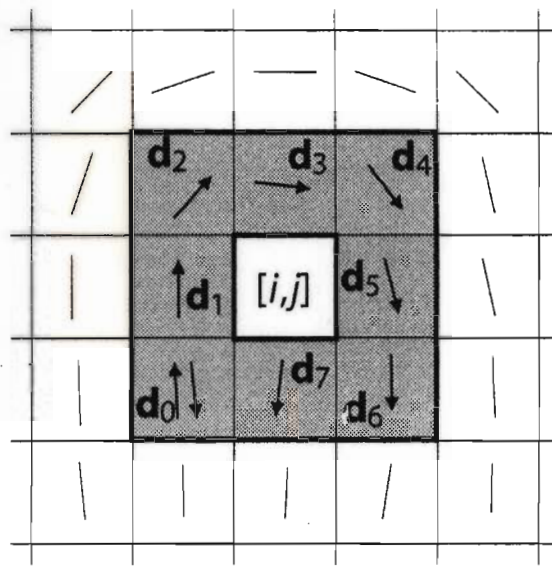
This now very easily gives us the minutiae. If we have retained the angle from earlier analysis we now have all minutiae including the angle info.

Poincaré index

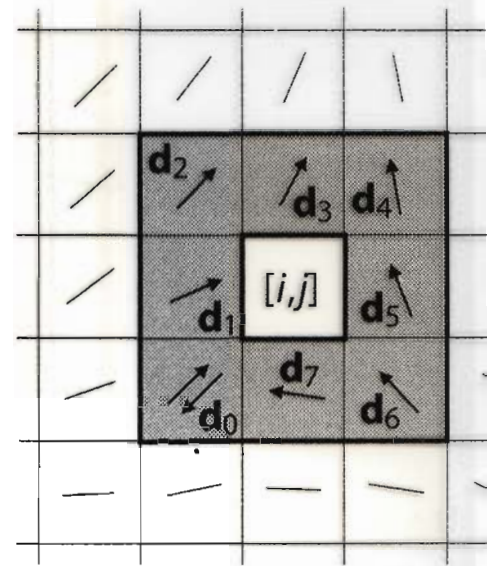
ph
21.7.08
(4)



$$P_{G,C}(i,j) = 360^\circ$$



$$P_{G,C}(i,j) = 180^\circ$$



$$P_{G,C}(i,j) = -180^\circ$$

re 2.13 Example of computation of the Poincaré index in the 8-neighborhood of po
ing (from the left to the right) to a whorl, loop and delta singularity, respectively. Note
e loop and delta examples (center and right), the direction of \mathbf{d}_0 is first chosen upward
ute the angle between \mathbf{d}_0 and \mathbf{d}_1) and then successively downward (when computing
e between \mathbf{d}_7 and \mathbf{d}_0) [21].

Combining the angle information around
a point allows us to classify

$$P(i,j) = \begin{cases} 0^\circ & \text{if } [i,j] \text{ not singular} \\ 360^\circ & \text{if } [i,j] \text{ is of whorl type} \\ 180^\circ & \text{if } [i,j] \text{ is of loop type} \\ -180^\circ & \text{if } [i,j] \text{ is a delta.} \end{cases}$$

Now we have:

- (a) a picture with one-pixel wide lines
- (b) Line endings and bifurcations marked
- (c) ridge direction
- (d) Poincaré index for each pixel

cpb
21.7.09
(5)



Figure 2.12 The detected minutiae features are superimposed on the original inked fingerprint for display.

Matching

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21.7.09

⑥



(a)



(b)



(c)

The computer tries to rotate, shift and rescale, maybe even distort to make as minutiae match as possible.

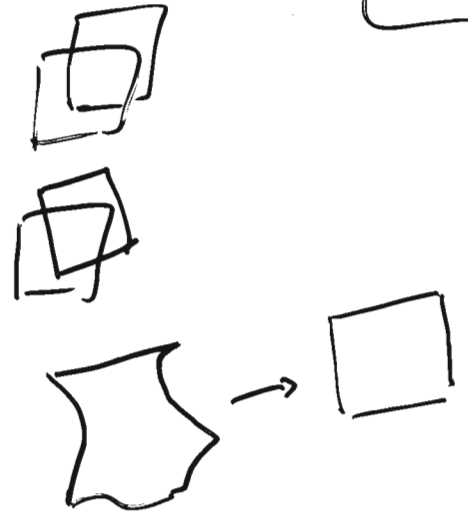
Run through the database and deliver good matches for further inspection.

Matching

cpb
22.7.05
①

Cave of:

- displacement
- rotation
- partial overlap
- nonlinear distortion
- pressure & skin condition
- noise
- feature extraction errors



Summary for fingerprint system

Start: Image

1. LACE
2. Gabor filtering including
 - (a) direction computation
 - (b) frequency computation
3. convert to 2-color at some threshold
4. thin out lines to 1-pixel-width.
5. determine minutiae incl. features
 - direction
 - Poincaré index

Then: match!

Further issues:

cpb
22.7.09
(2)

- interoperability
- "Daubert" questions
Validity in court?

[1993 US supreme court
Daubert vs. Merrell Dow Pharm. ac.]

Applications

- electronic passport, border control
- access control
 - places, buildings, areas...
 - notebooks, ...
 - mobile phones, ...
 - cars...
- criminal investigations
- welfare fraud reduction
- driver registration



SUMMARY

cpb
22.7.08
(3)

o Introduction

o Cryptography

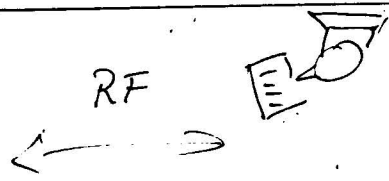
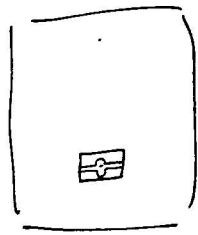
- digital signatures
- group theory
- key exchange, DH
- AES, DES
- hash functions
- PKI, certificate, directory ^{services}, CA
- SECURITY models

o ePassport

- passive & active authentication
- Doc 9303
 - data structure, communication + protocols, MRZ, Basic Access Control, Security Object
 - Extended Access Control → Chip authentication (repl. Active Authentication and has DH), Terminal authentication

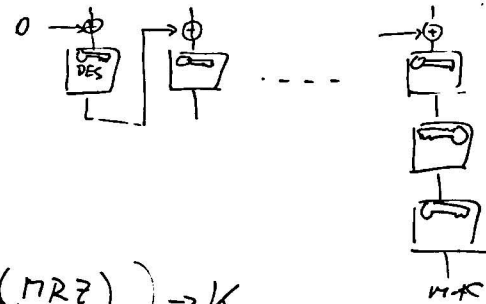
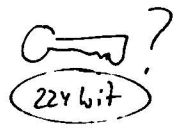
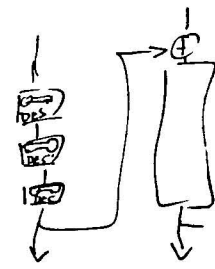
o Biometrics, Fingerprints

- History, and classification
- Automation
 - image quality enhancement, ...

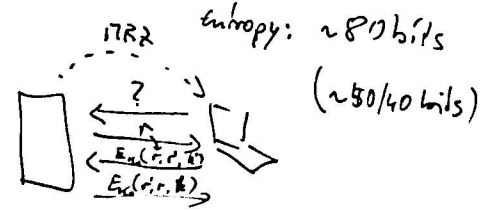
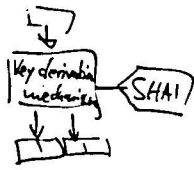


Encryption: 2-TDES (AES?)

Authentication: retail (CMAC)



BAC: key derivation (SHA1(MRZ)) $\rightarrow K_0$



key derivation (K || K') $\rightarrow K$

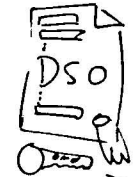
Chip Authentication (EAC)

$\equiv \text{DH}$ Key exchange
key derivation (xyP) $\rightarrow K_{2M}$

$(P, xP, yP) \xrightarrow{?} xyP$
Diffie-Hellman-Problem

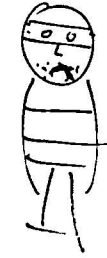
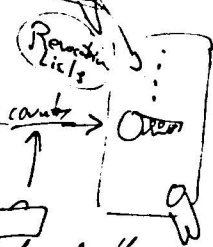
Passive Authentication

• Chip uses static key pair: (X, XP)



Terminal checks signature (ECDSA)

& that the hash of XP is correct.



Check Signatures based on a cloned Root-CA

Verify.

Terminal Auth.

