# Advanced cryptography: Pairing-based cryptography winter term 2012/13 

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## 5. Exercise sheet <br> Hand in solutions until Monday, 26 November 2012, 23:59:59

## Exercise 5.1 (Some reductions).

Consider the setup from the lecture: We have two groups $G_{1}$ and $G_{3}$ with $\# G_{1}=\# G_{3}=\ell$ prime and a pairing $e: G_{1} \times G_{1} \rightarrow G_{3}$.
(i) Show that $\mathrm{DBDH} \leq \mathrm{DDH}_{G_{3}}$.
(ii) Show that $\mathrm{DL}_{G_{3}} \equiv\left(\mathrm{DL}_{G_{1}}\right.$ and GTI).

## Exercise 5.2 (Man-in-the-middle).

Consider the Joux's three party key-exchange protocol. Show that the proto- 7 col is vulnerable to man-in-the-middle attacks, i.e. describe how a malicious fourth party can modify the protocol to be afterwards able to intercept all communication.

## Exercise 5.3 (Notions).

Explain why we call Smart's key agreement protocol "authenticated".

Exercise 5.4 (A simple proof).
Show that the forward-security of Smart's authenticated key agreement proto- 4 col can be reduced to the BDH problem and vice versa.

