Esecurity: secure internet & e-voting, summer 2013 MICHAEL NÜSKEN

3. Exercise sheet Hand in solutions until Monday, 29 April 2013, 10:00

Exercise 3.1.

Exercise 3.2 (X.509).

Read RFC 5280 and answer the following questions:

- (i) What classes of certificates are there?
- (ii) What is the basic syntax of X.509 v3 certificates? Describe the 2 Certificate Fields in detail. Which signature algorithms are supported?
- (iii) What is a trust anchor? Can one use different trust anchors?
- (iv) What conditions are satisfied by a prospective certification path in the 2 path validation process?

Exercise 3.3 (Security estimate). (0+8 points)

RSA is a public-key encryption scheme that can also be used for generating signatures. It is necessary for its security that it is difficult to factor large numbers (which are a product of two primes). The best known factoring algorithms achieve the following (heuristic, expected) running times:

(8 points)

(0 points)

2

2

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method	year	time for <i>n</i> -bit integers
trial division	$-\infty$	$\mathcal{O}^{\sim}\left(2^{n/2} ight)$
Pollard's $p-1$ method	1974	$\mathcal{O}^{\sim}(2^{n/4})$
Pollard's <i>o</i> method	1975	$\mathcal{O}^{\sim}(2^{n/4})$
Pollard's and Strassen's method	1976	$\mathcal{O}^{\sim}\left(2^{n/4} ight)$
Morrison's and Brillhart's continued fractions	1975	$2^{\mathcal{O}(1)n^{1/2}\log_2^{1/2}n}$
Dixon's random squares	1981	$2^{(\sqrt{2}+o(1))n^{1/2}\log_2^{1/2}n}$
Lenstra's elliptic curves method	1987	$2^{(1+o(1))n^{1/2}\log_2^{1/2}n}$
quadratic sieve		$2^{(1+o(1))n^{1/2}\log_2^{1/2}n}$
general number field sieve	1990	$2^{((64/9)^{1/3} + o(1))n^{1/3}\log_2^{2/3}n}$

It is not correct to think of o(1) as zero, but for the following rough estimates just do it, instead add a O(1) factor. Factoring the 768-bit integer RSA-768 needed about 1500 2.2 GHz CPU years (ie. 1500 years on a single 2.2 GHz AMD CPU) using the general number field sieve. Estimate the time that would be needed to factor an *n*-bit RSA number assuming the above estimates are accurate with o(1) = 0 (which is wrong in practice!)

- (i) for n = 1024 (standard RSA),
- (ii) for n = 2048 (as required for Document Signer CA),
- (iii) for n = 3072 (as required for Country Signing CA).
- (iv) Now assume that the attacker has 1000 times as many computers and 1000 times as much time as in the factoring record. Which n should I choose to be just safe from this attacker?

Repeat the estimate assuming that only Pollard's ρ method is available

+1	
+1	
+1	

+1

+1

+1

+2

- (v) for n = 1024,
- (vi) for n = 2048,
- (vii) for n = 3072.

Remark: The statistics for discrete logarithm algorithms are somewhat similar as long as we consider groups \mathbb{Z}_p^{\times} . For elliptic curves (usually) only generic algorithms are available with running time $2^{n/2}$.