Cryptography, winter 2015/16

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7. Exercise sheet
Hand in solutions until Saturday, 19 December 2015, 12:00

Exercise 7.1 (PRF $\Rightarrow$ PRG). (4+4 points)

Let $F\colon \{0,1\}^\kappa \to \{\{0,1\}^\kappa \to \{0,1\}^\kappa\},\ k \mapsto F_k$ be a pseudorandom function. Fix $w_0, w_1, w_2 \in \{0,1\}^\kappa$. Define $G(s) := F_s(w_0)|F_s(w_1)|F_s(w_2)$. 4+4

Prove that G is a pseudorandom generator.

Exercise 7.2 (IND-CPA?). (12 points)

Let F be a pseudorandom function and G a pseudorandom generator with expansion factor $\ell(\kappa) = \kappa + 1$. For each of the following encryption schemes, classify the scheme is insecure, IND-POA secure (but not IND-CPA) or IND-CPA secure. In each case, the shared key k is chosen unformly random, $k \in \{0,1\}^\kappa$.

(i) To encrypt $m \in \{0,1\}^{2\kappa+2}$ send $m \oplus (G(k)|G(k+1))$. 3

(ii) To encrypt $m \in \{0,1\}^{\kappa+1}$ chooose a random $r \xleftarrow{\$} \{0,1\}^\kappa$ and send $[r, G(r) \oplus m]$. 3

(iii) To encrypt $m \in \{0,1\}^\kappa$ send $m \oplus F_k(0^\kappa)$. 3

(iv) To encrypt $m \in \{0,1\}^{2\kappa}$ chooose a random $r \xleftarrow{\$} \{0,1\}^\kappa$ and send $[r, m \oplus (F_k(r)|F_k(r+1))]$. 3

Even if not mentioned explicitly: any statement needs a proof.